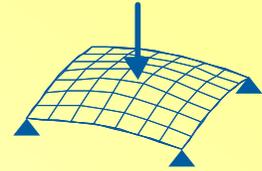


Cyklus prednášok pod záštitou rektora STU  
Lecture series under the auspices of STU rector

**WIP**  
siting professors'  
College **STU**



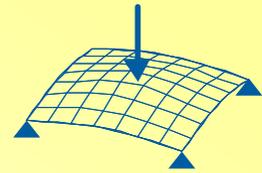
# Mechanics and applications of multifunctional materials and structures

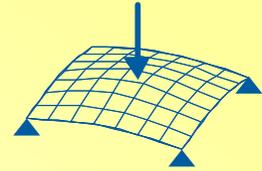
Prof. Dr.-Ing. habil. Dr. h. c. Chuanzeng Zhang  
Chair of Structural Mechanics, School of Science and Technology,  
University of Siegen, Germany



Siegen

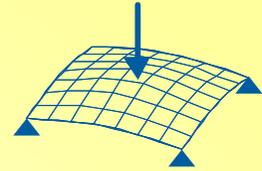
# Where is Siegen?





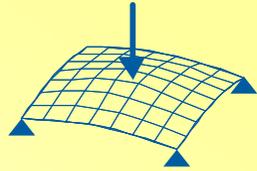
- Fracture analysis of FGMs
- Fracture analysis of smart materials
- Wave propagation in smart structures
- Wave propagation in phononic crystals
- Sensitivity analysis of damaged structures
- Computational mechanics

# OUTLINE



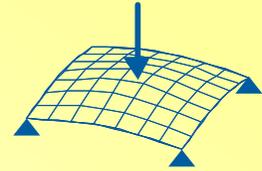
- Physical motivation
- Functionally graded materials (FGMs) and structures
- Phononic crystals (PCs) and structures
- Smart materials and structures
- Conclusions

Visiting Professors' College STU, Bratislava, Slovakia, 14 May 2015

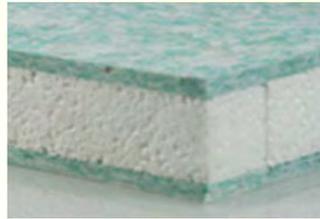


# Physical motivation

# Multifunctional materials



Mechanical loading



Super high temperature

Wear

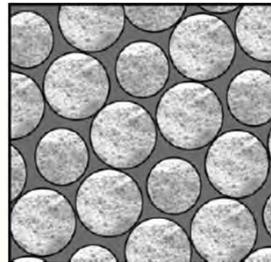
Corrosion

Noise protection



Oxidation

Light transmission and reflection



Chemical loading

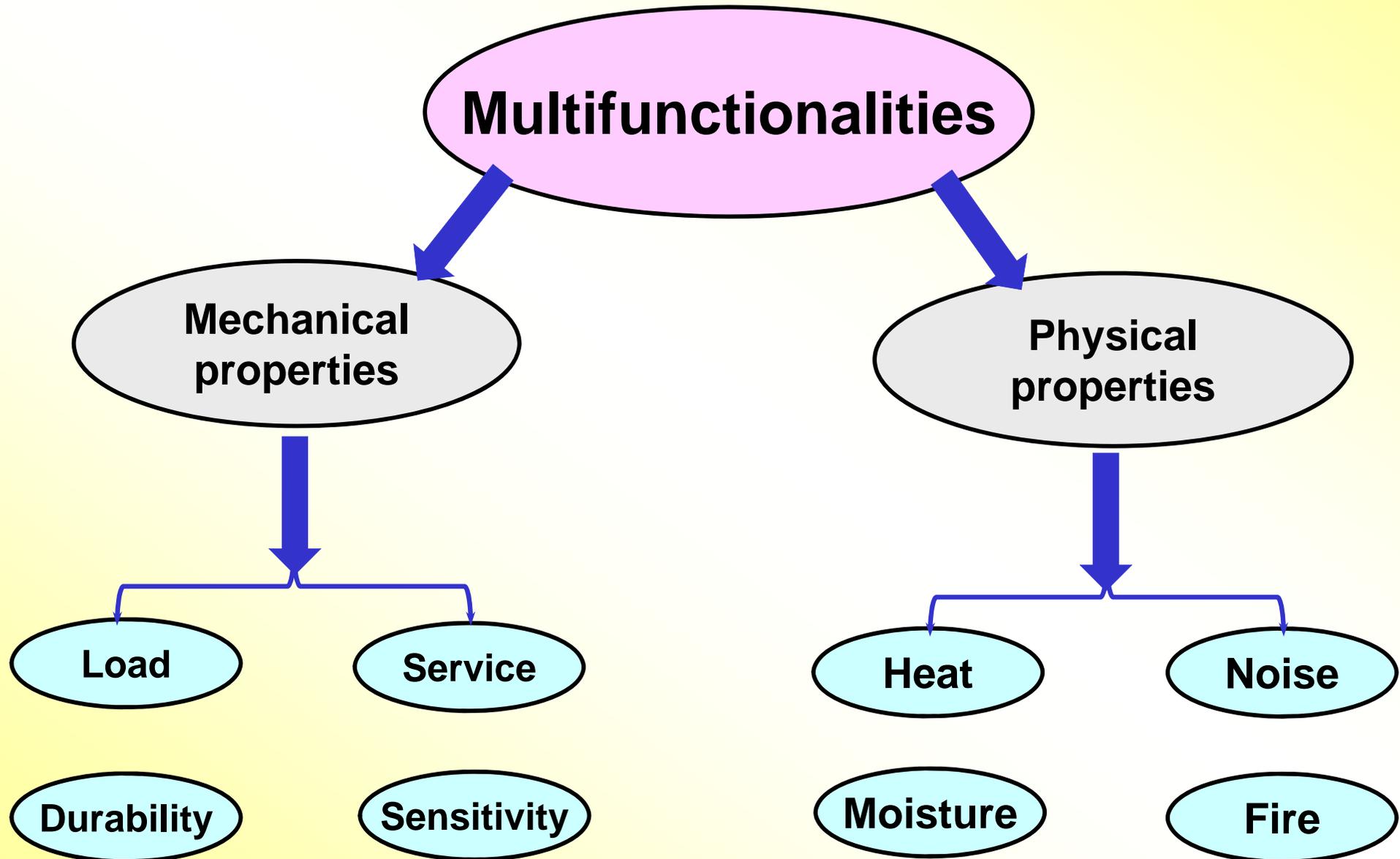
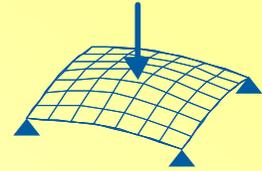
Radioactivity

Electric and magnetic loading

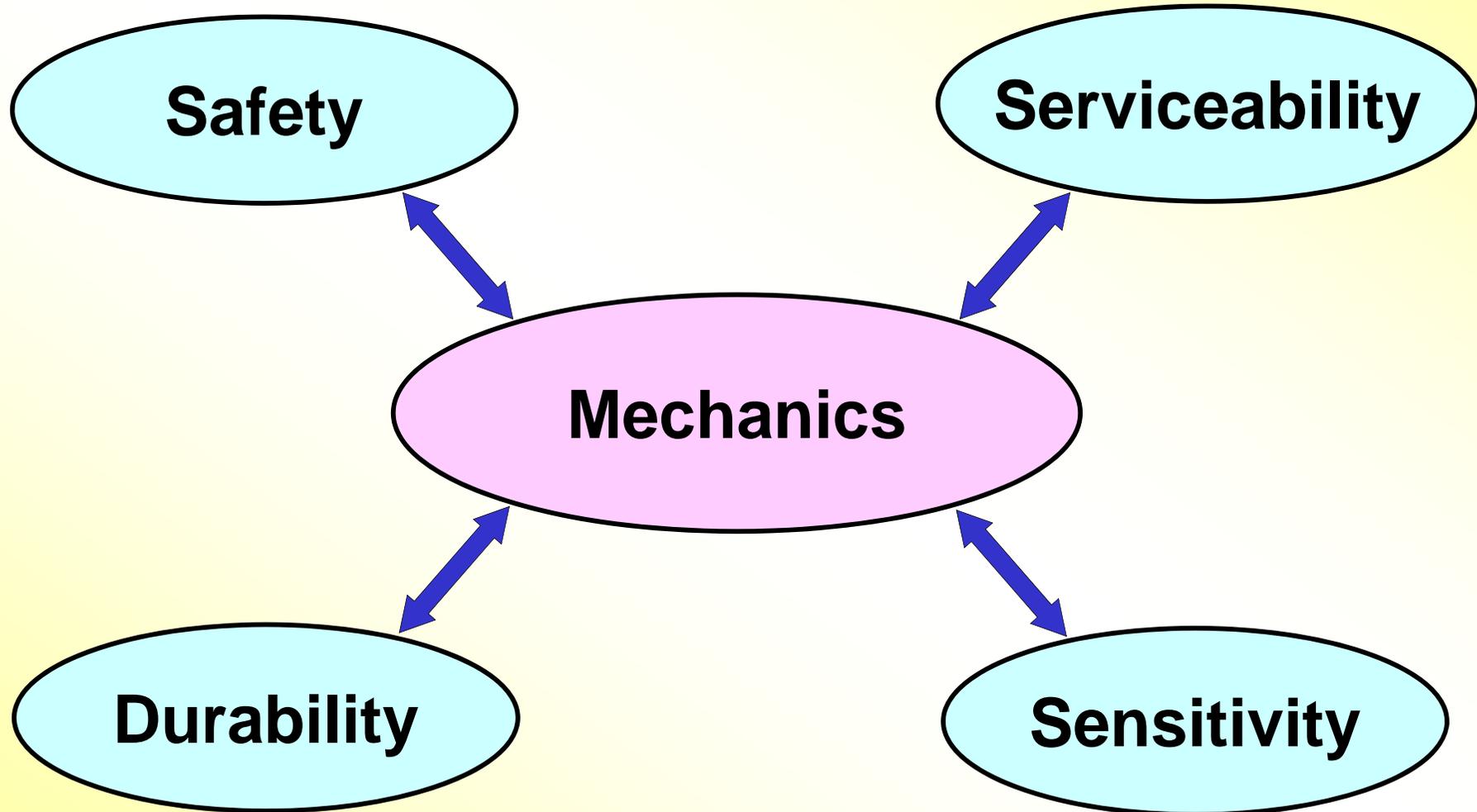
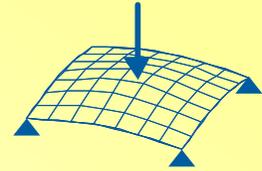
Biological compatibility

**A single material phase cannot satisfy all these requirements!**

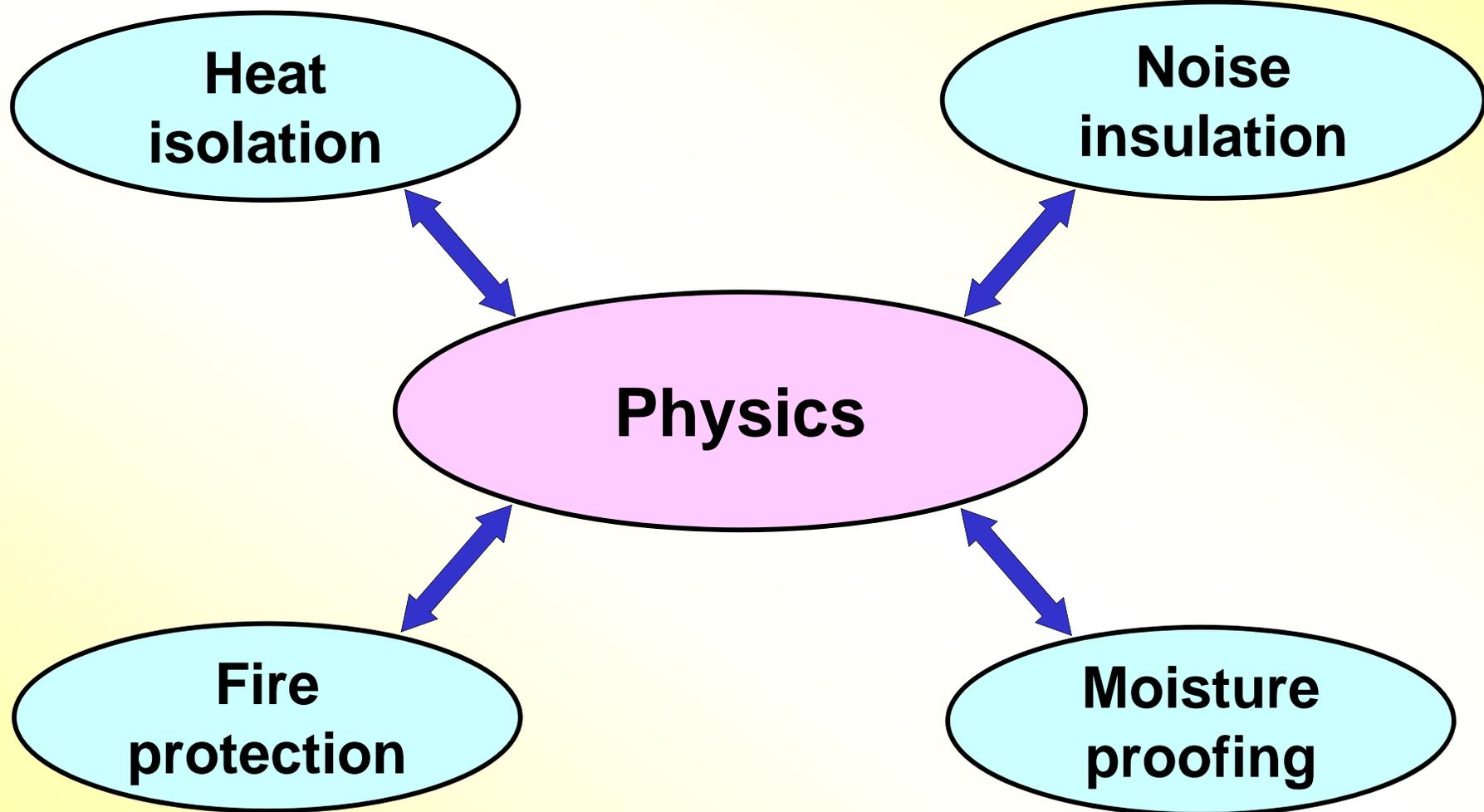
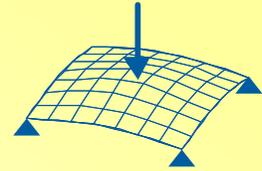
# What does „multifunctional“ mean?

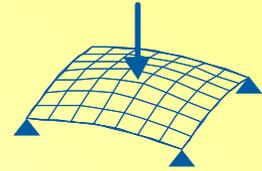


# Multifunctionalities



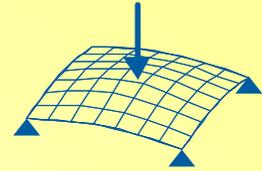
# Multifunctionalities





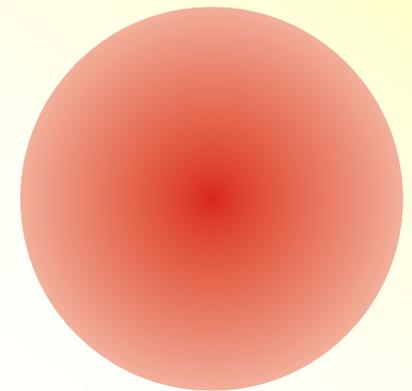
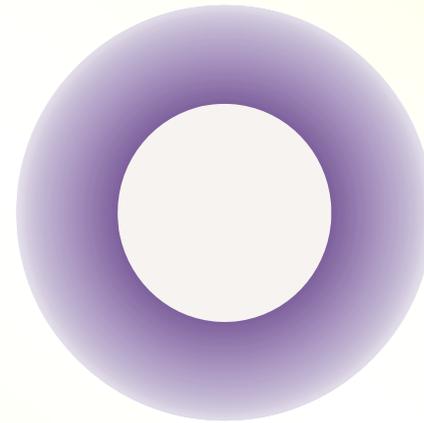
# Functionally graded materials (FGMs) and structures

# Why Functionally Graded Materials (FGMs)?

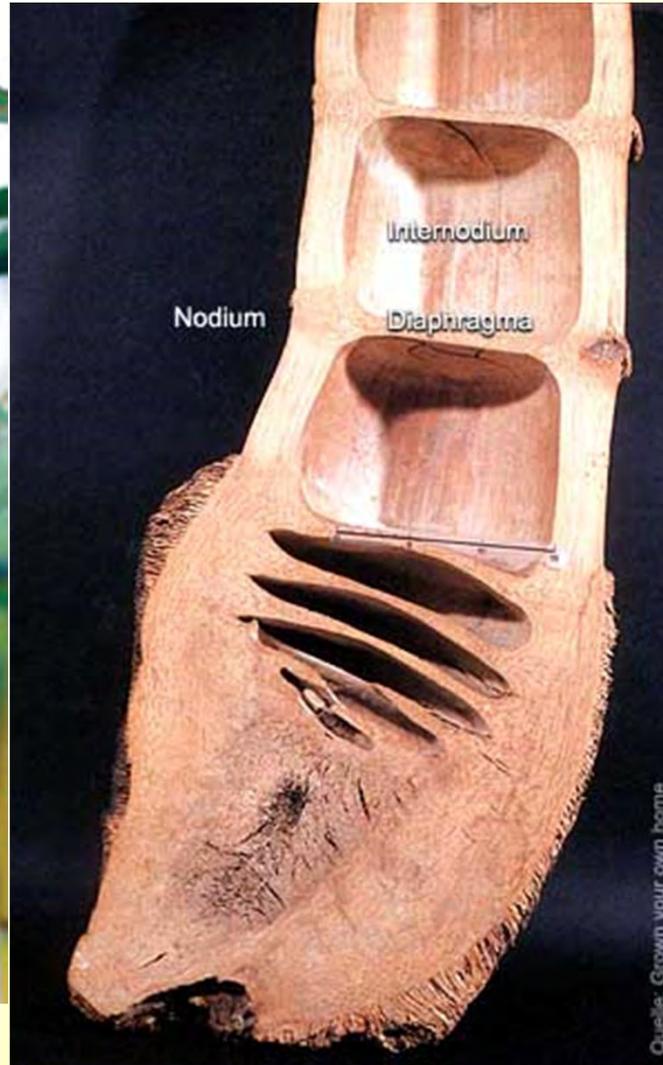
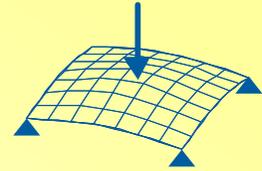


## Functionally Graded Materials (FGMs):

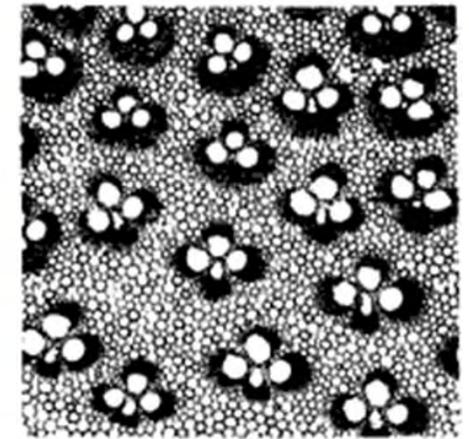
- Advanced functional composites
- Continuous profile of materials constituents
- Material constants change continuously in space



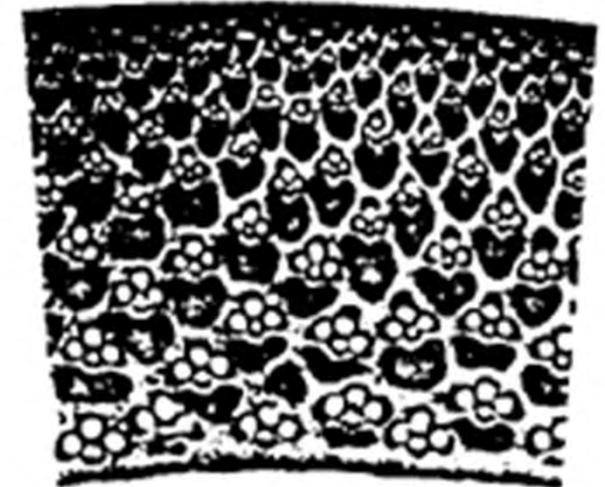
# FGMs: Lesson from nature



Fiber

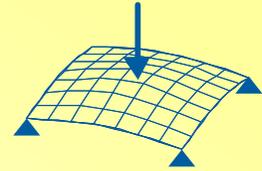


out side

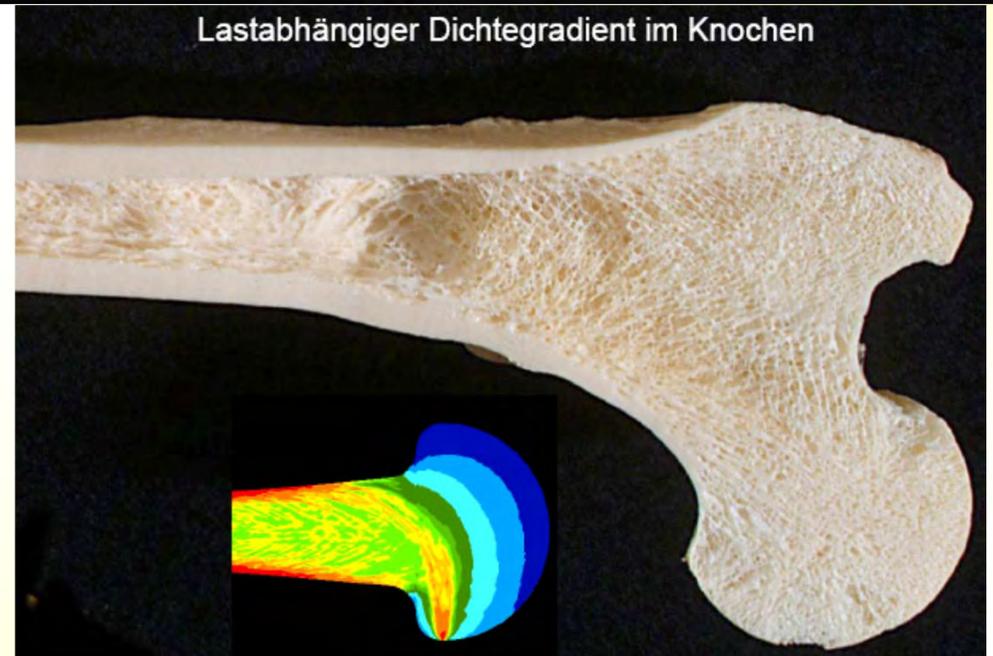


inner side

# FGMs: Lesson from nature



Oberschenkelknochen



Lastabhängiger Dichtegradient im Knochen

# Innovative applications of FGMs and structures

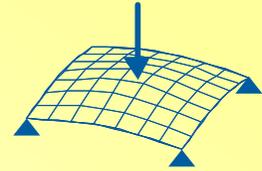
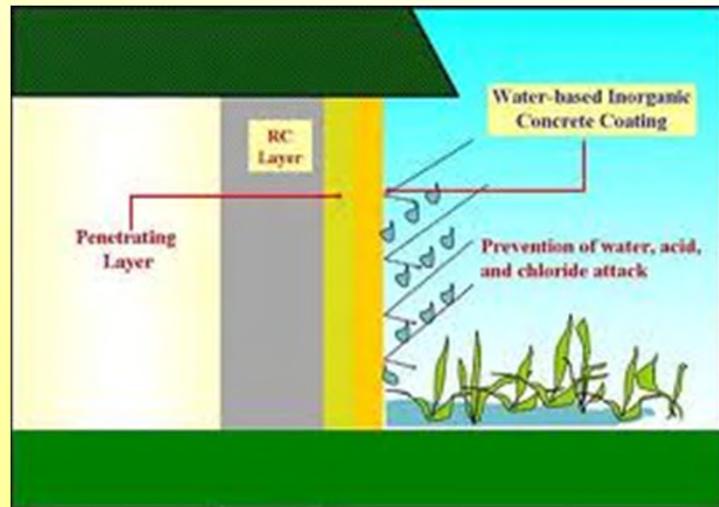
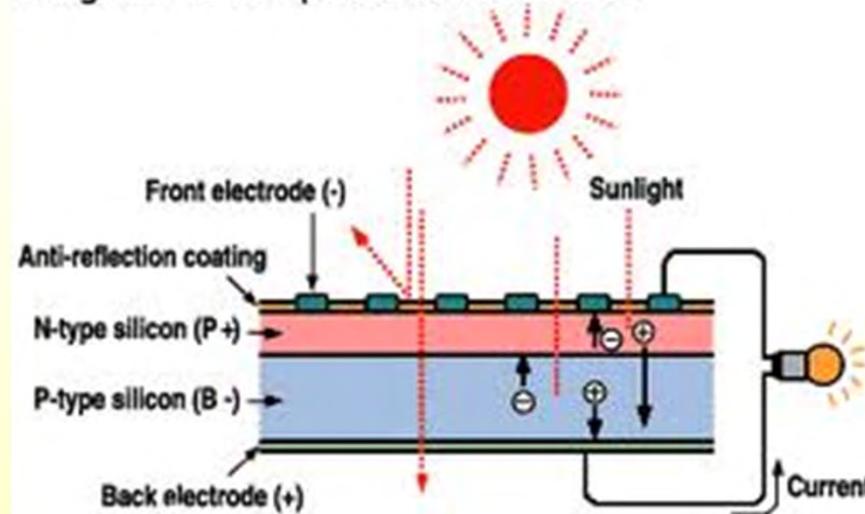
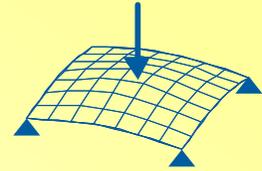


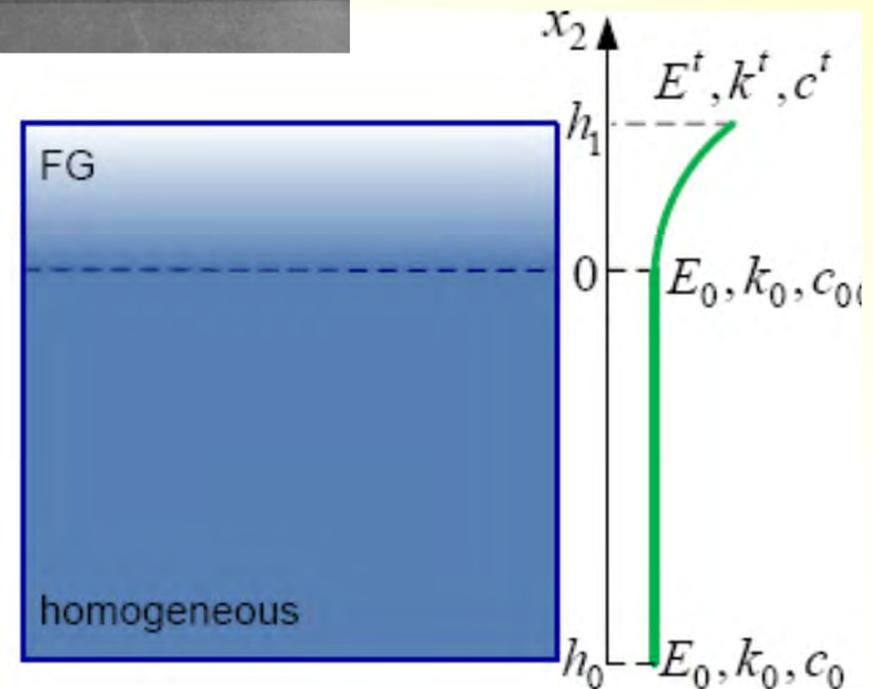
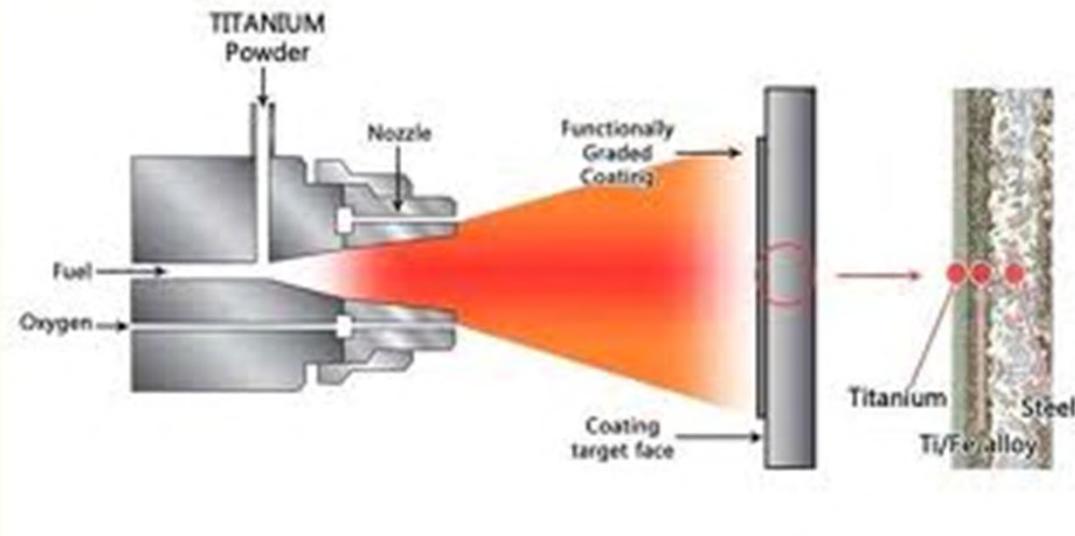
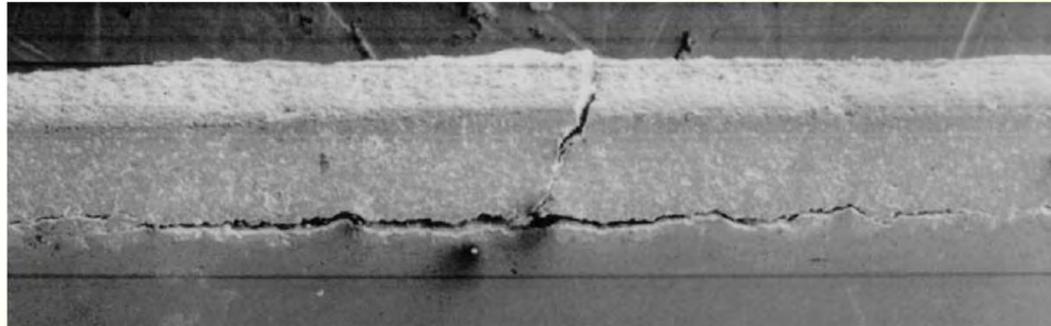
Diagram 1. The photovoltaic effect



# Mechanics of FGMs and structures

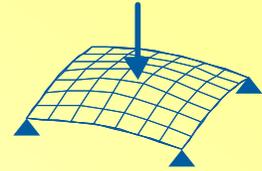


## Problem: Interface cracking !



FG coating

# Applications of FGMs and structures

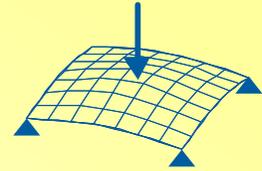


## **Important applications:**

Thermal barrier coating for severe temperature conditions.

## **Objectives of our works:**

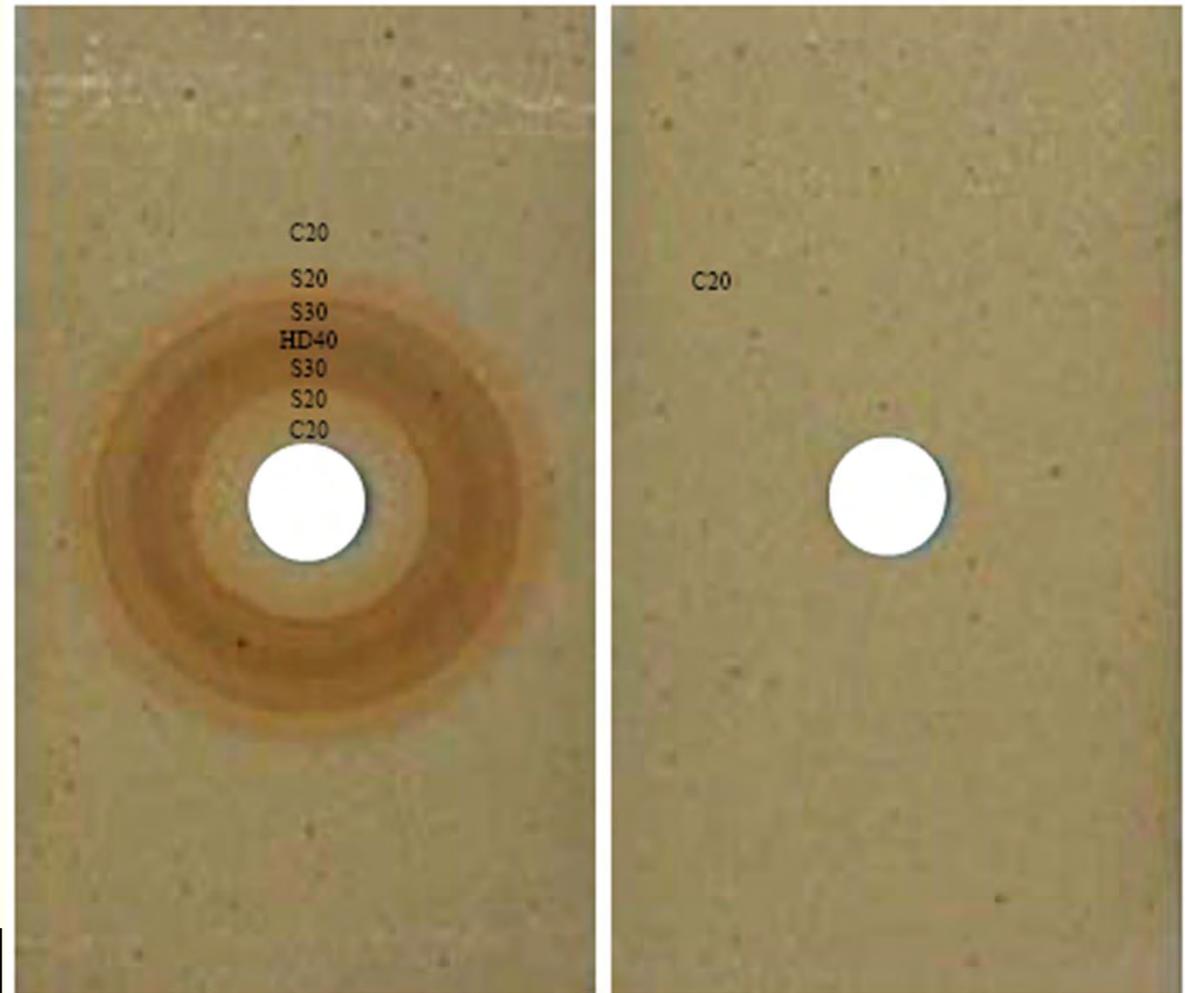
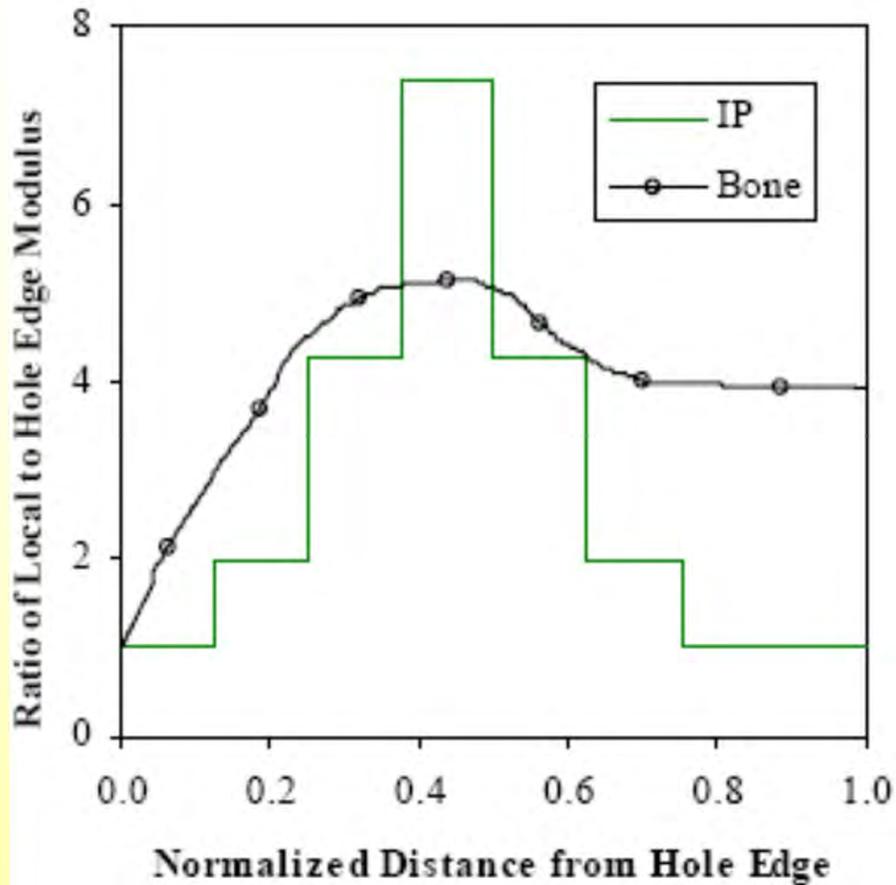
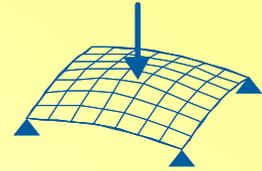
Crack analysis for thermal shock loading and impact loading!



- **Natural holes (foramina) exist in all bones to allow blood vessels to pass through their hard outer shells.**
- **Foramina never appear as fracture sites clinically or in laboratory tests of hole bones.**



# How bones design and adapt holes?

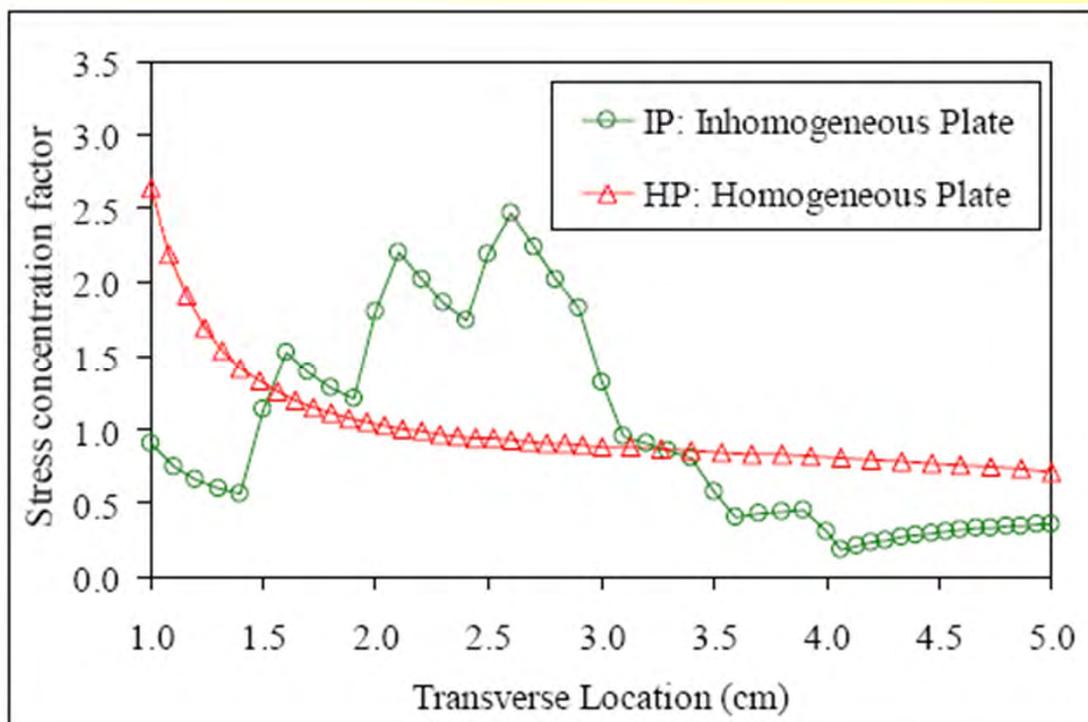
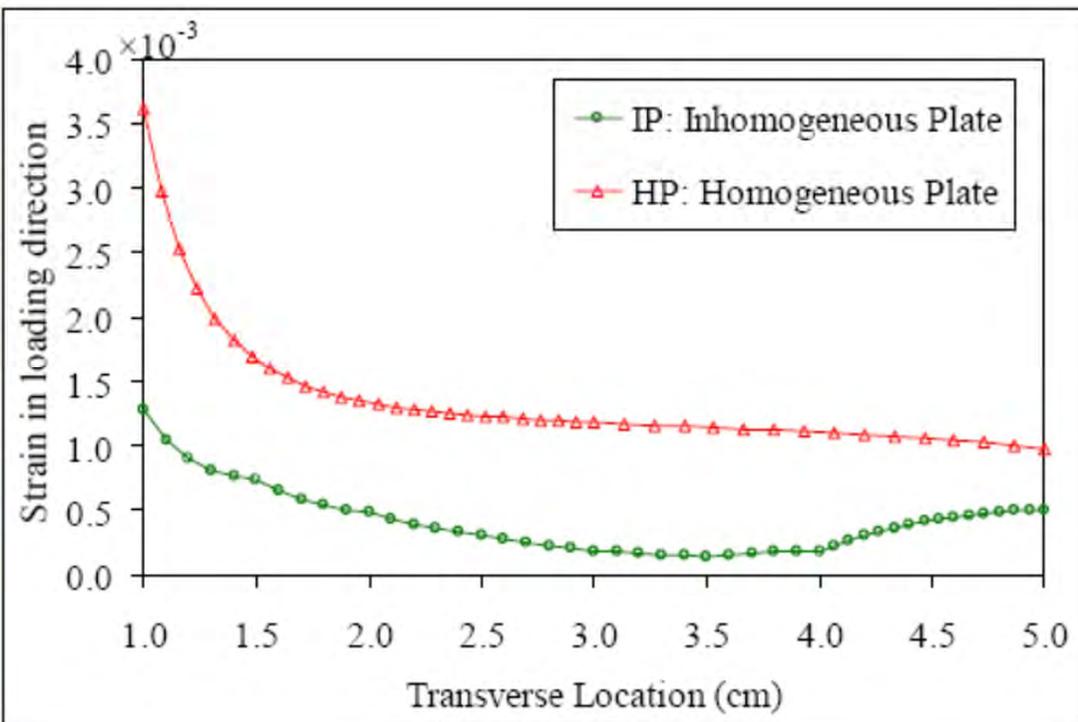
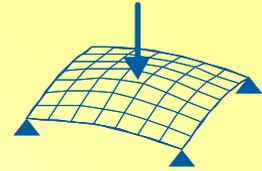


**Local modulus distribution**

(Buskirk et al., 2002)

**Biomimetic plate**

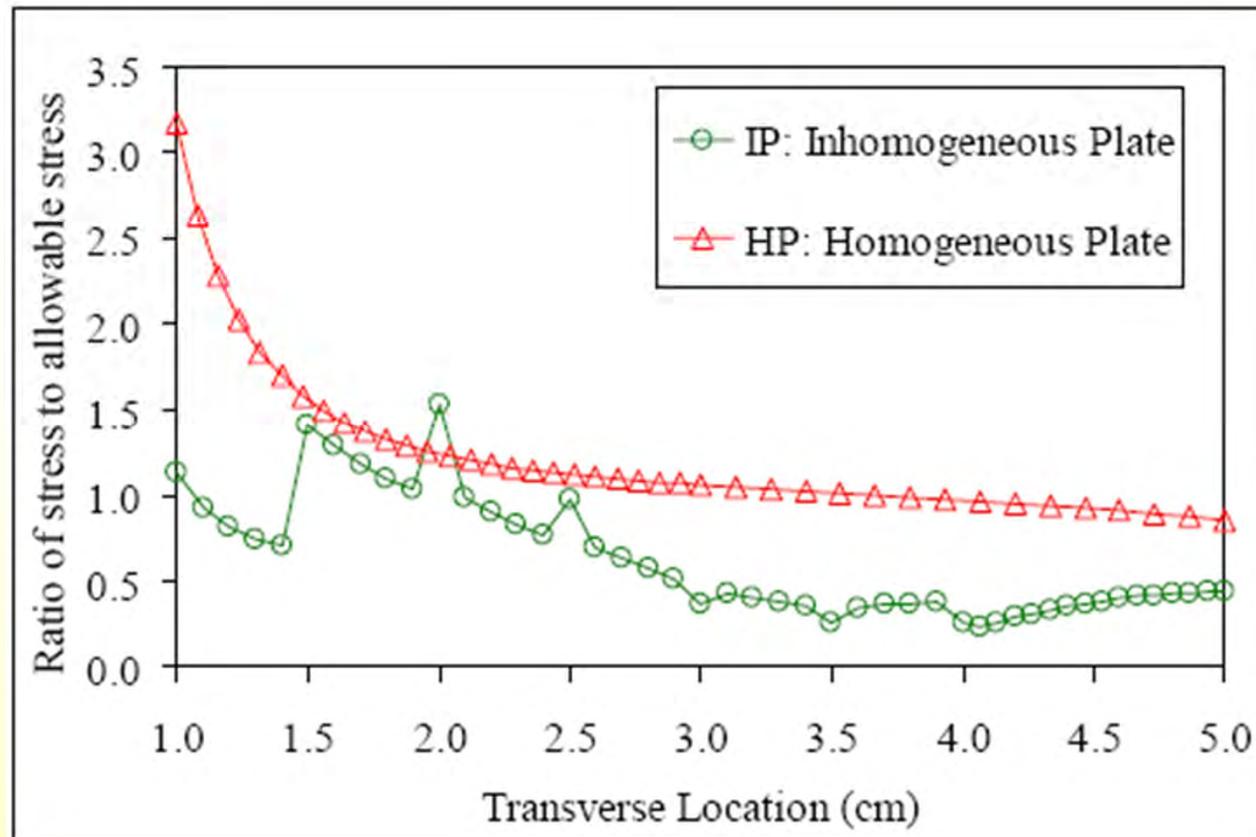
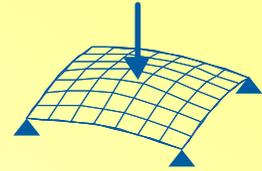
# Biological design of a hole



**Strain distribution**

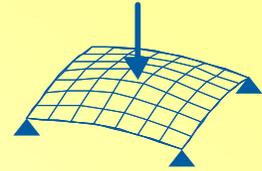
**Stress distribution**

# Biological design of a hole



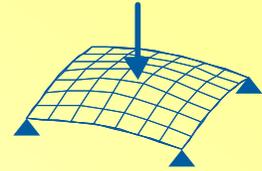
**Stress failure index (load carrying capacity)**

# Key questions



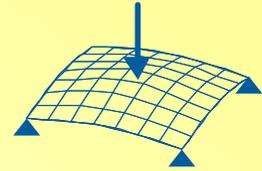
- **How to learn from nature materials?**
- **Can we design FGMs which allow holes but without stress concentration?**
- **Can we design FGMs which allow cracks but without or with reduced failure risk?**

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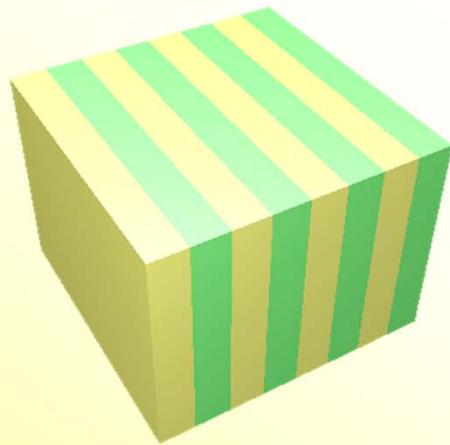
# Phononic crystals (PNCs) and structures

# Wave propagation in phononic crystals

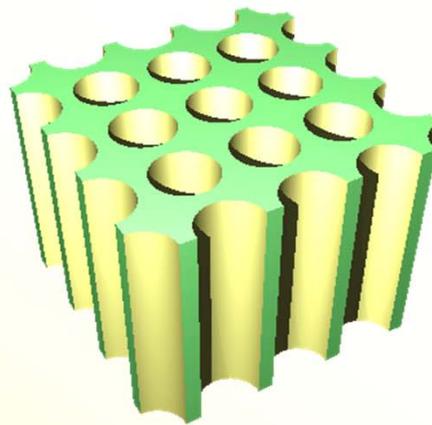


## Phononic crystals

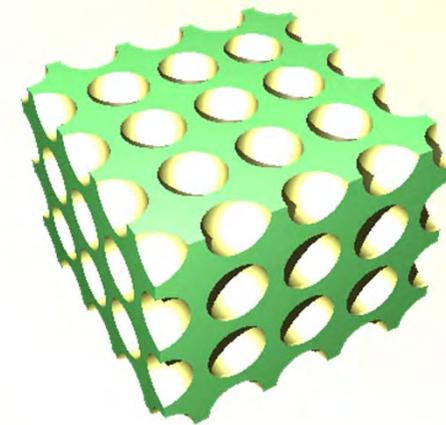
Composite materials composed of periodic arrangement of more than two materials with different elastic properties.



1-D



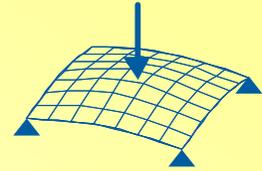
2-D



3-D

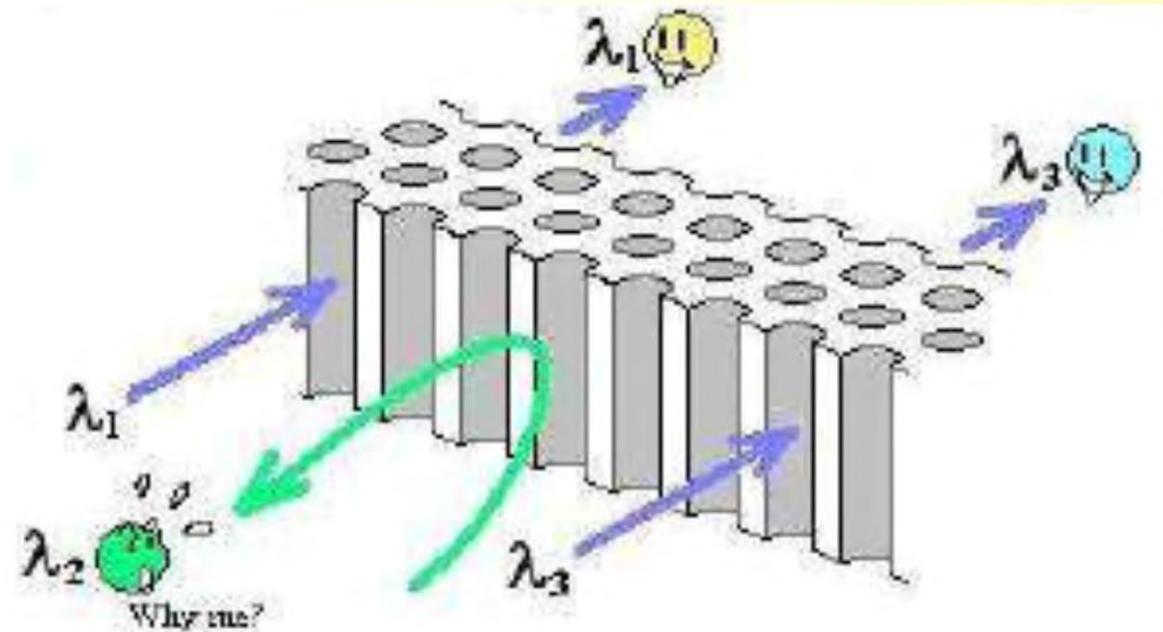
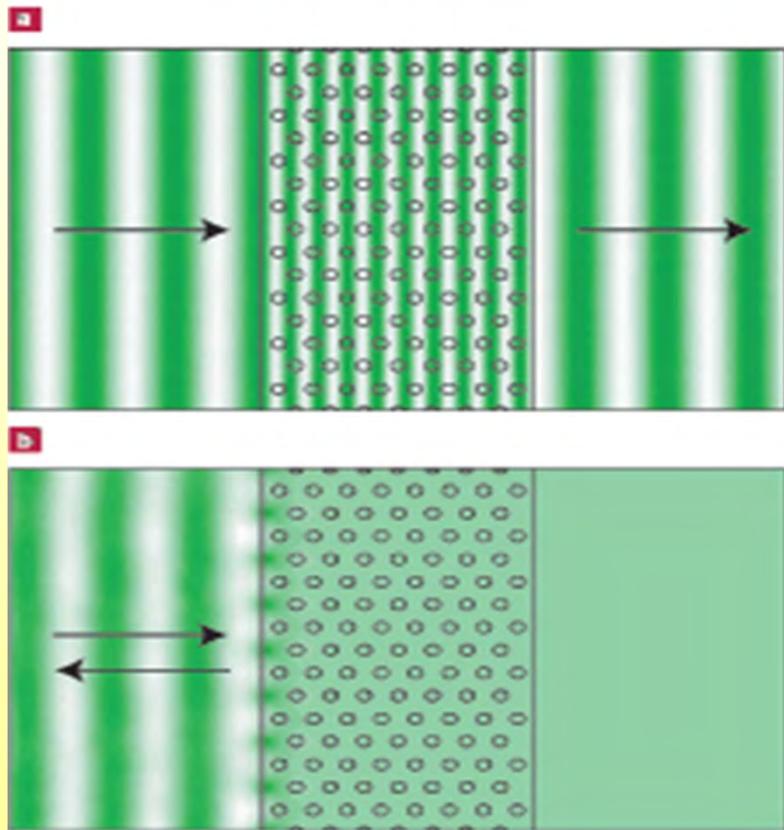
Phononic crystals may have **frequency band gaps!**

# Wave propagation in phononic crystals

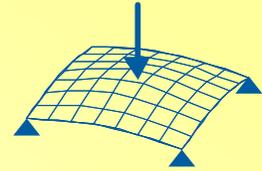


**Band-gap:** Frequency range, in which the propagation of elastic waves is prohibited.

**Innovative applications:** Acoustic filter, vibration isolation, noise reduction.

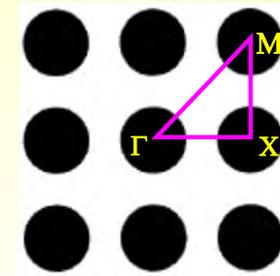


# Band-gaps (stop bands)



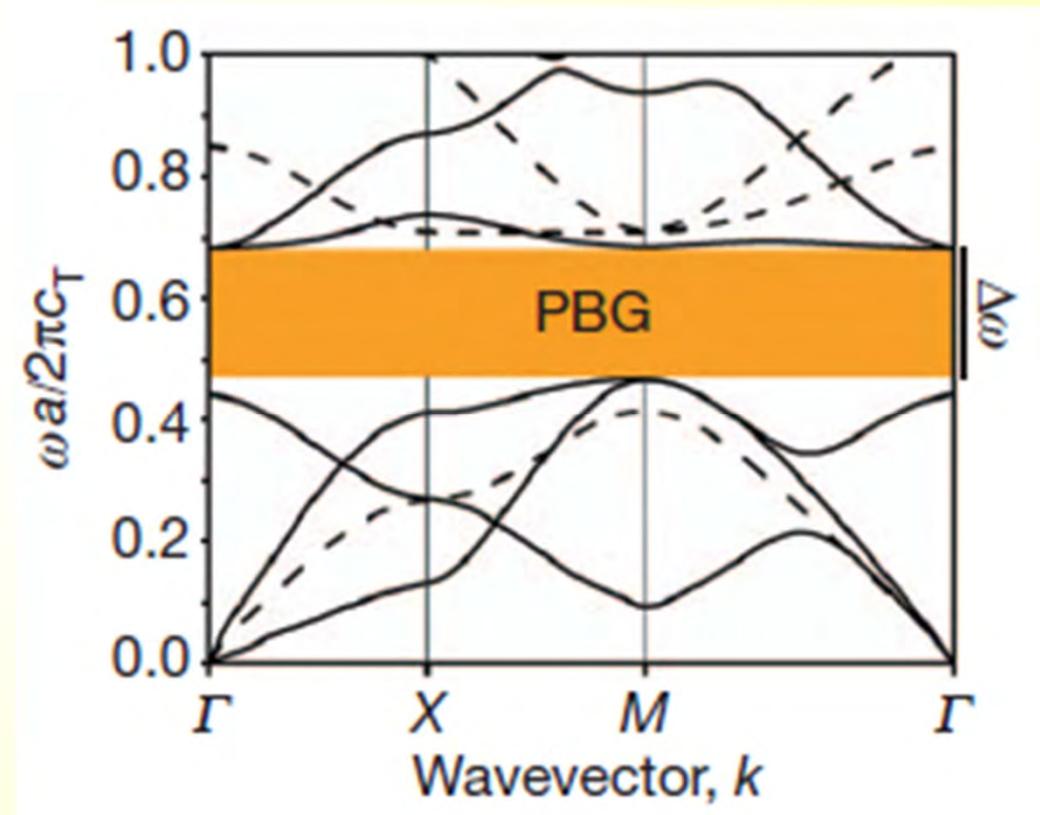
Elastic wave propagating in phononic crystals:

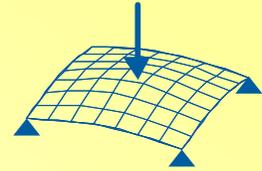
- Pass band
- Stop band: band-gap (PBG)



Mechanisms of band-gaps:

- Bragg scattering
- Local resonances





## Applications:

- Noise reduction
- Vibration damping
- Design of new acoustic devices
- ...

## Nanoscale phononic crystals:

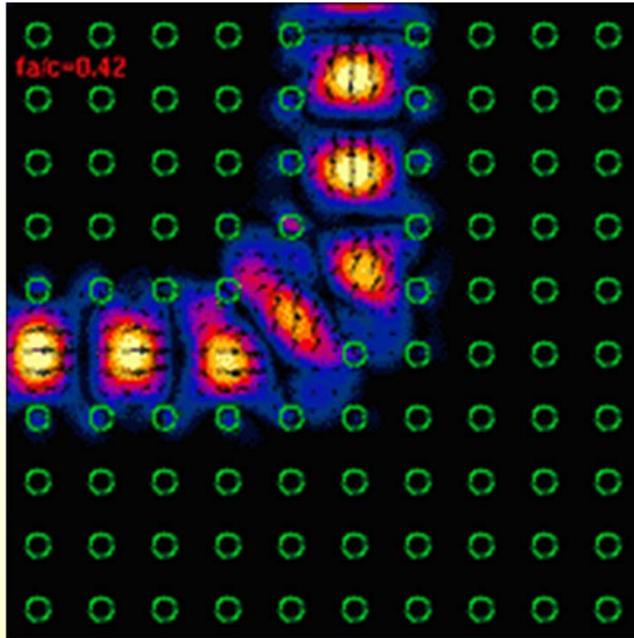
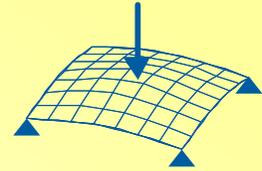
### Hypersonic phononic crystals

- Acousto-optical modulation
- Electron-phonon engineering
- Heat management
- ...

Phys. Rev. Lett. 94, 115501, 2005

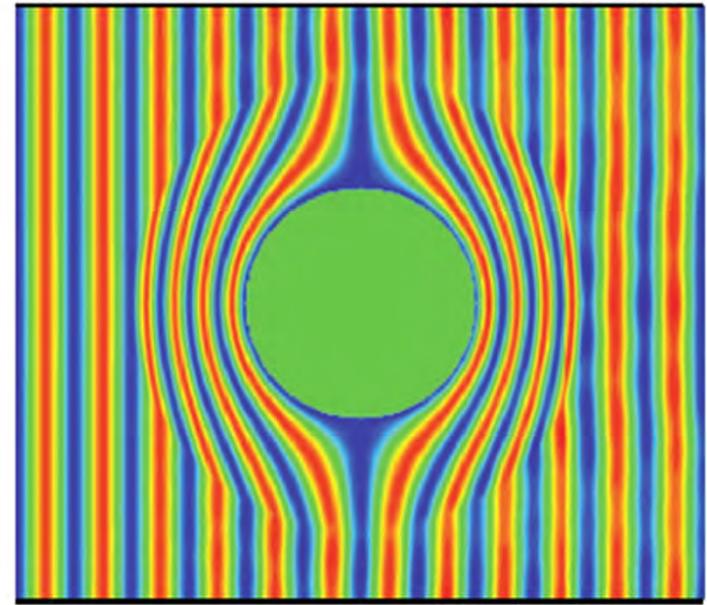
Phys. Rev. Lett. 101, 033902, 2008

# Innovative applications

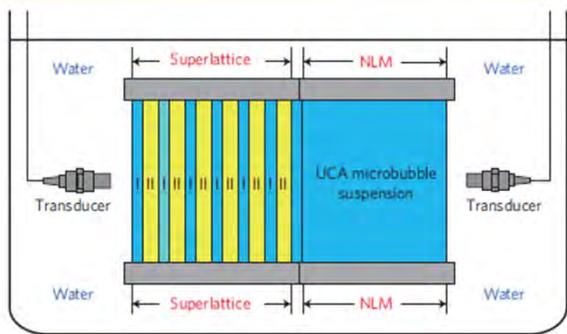


Wave bending

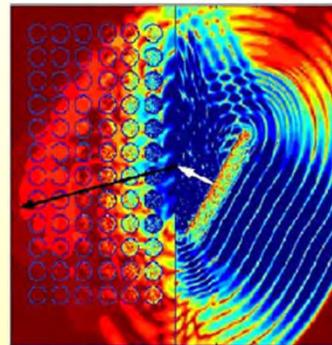
Sound wave  
→



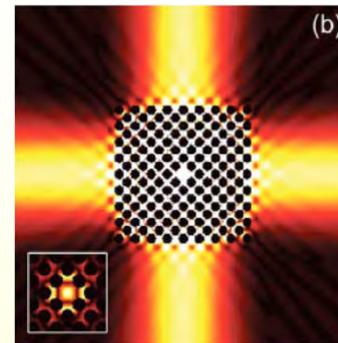
Acoustic cloaking



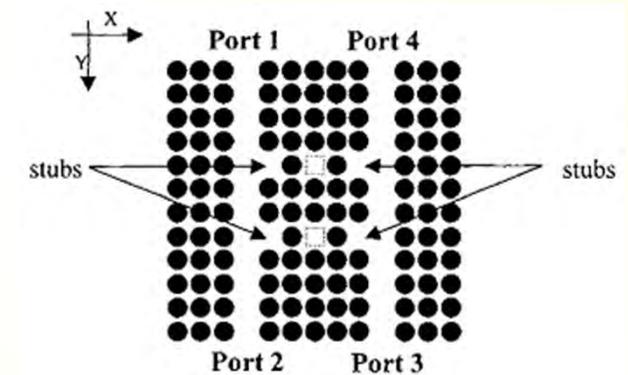
Acoustic diode



Negative refraction

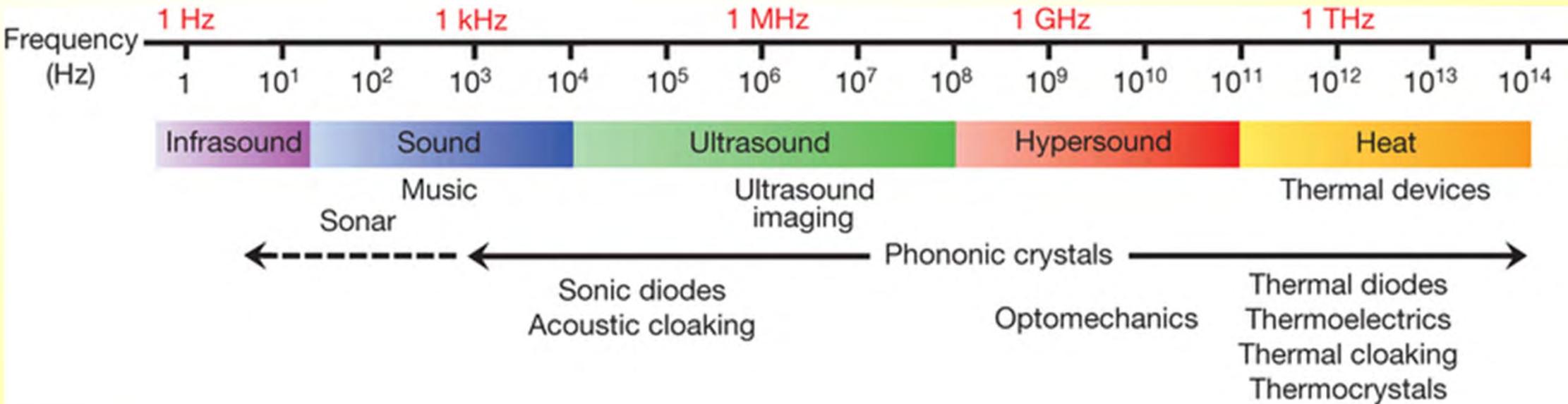
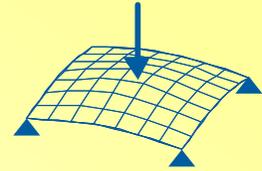


Wave guide



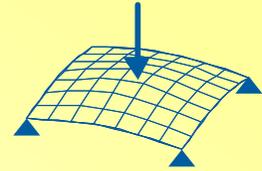
Phonic coupler

# Phononic spectrum



**Martin Moldovan: *Nature* 2013, 503: 12608**

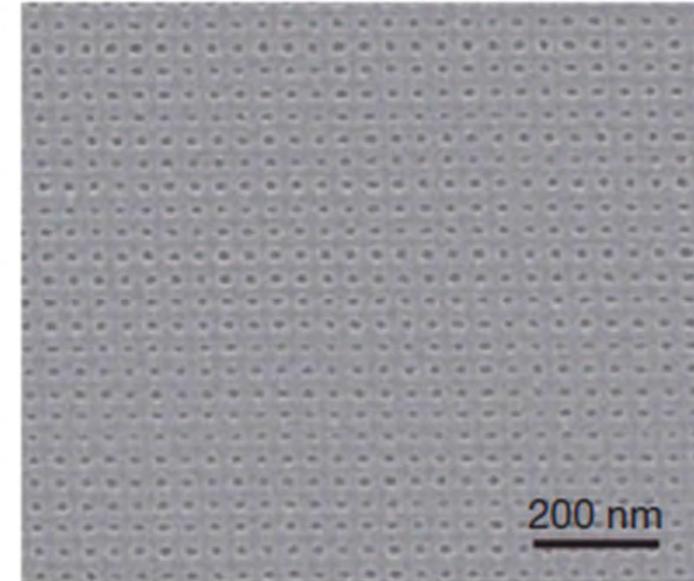
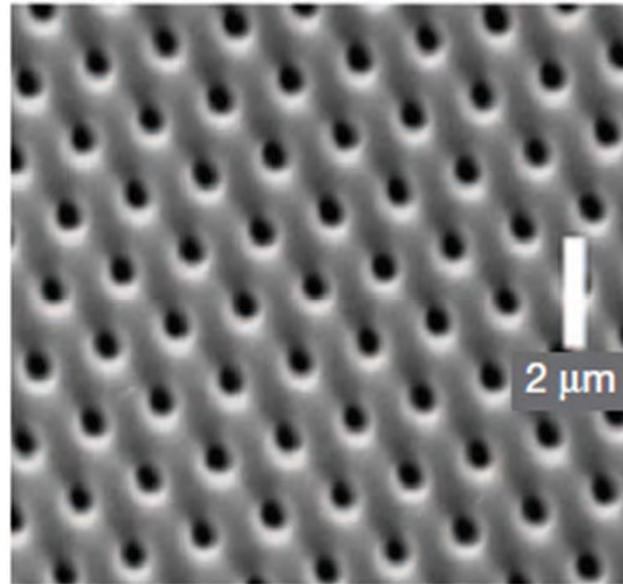
# From macroscale to nanoscale



Sound

Hypersound

Heat



kHz

GHz

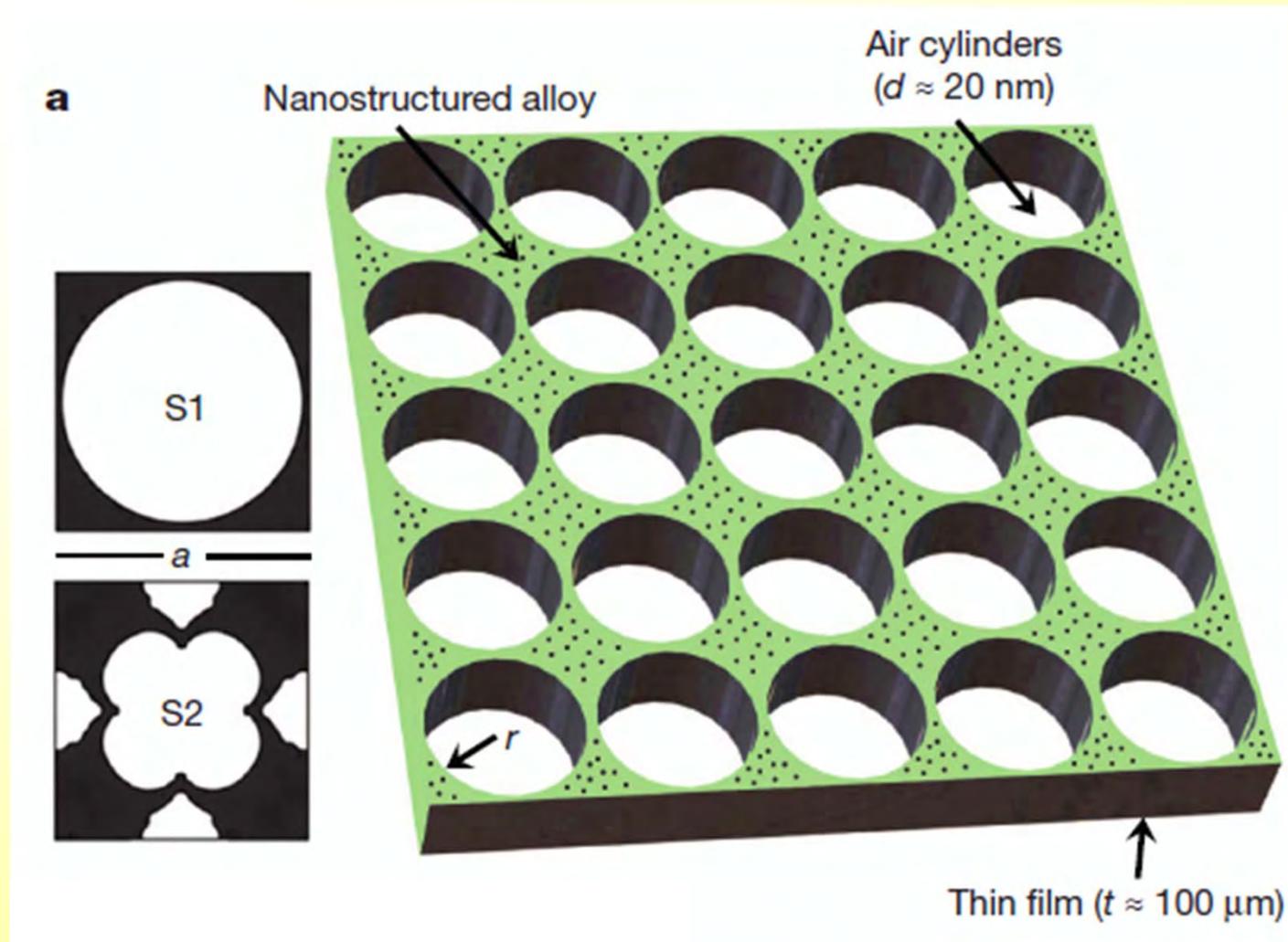
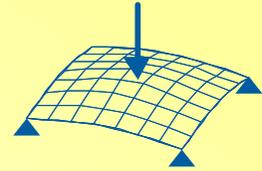
THz

Macroscale

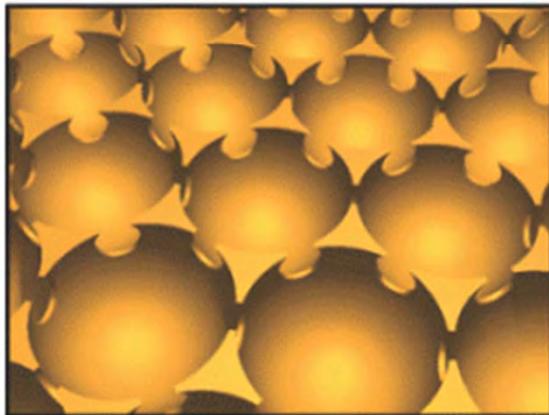
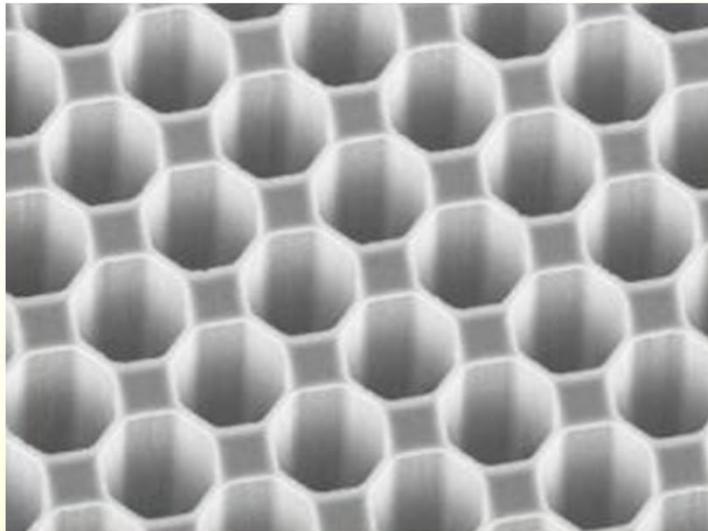
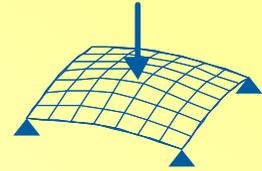
Microscale

Nanoscale

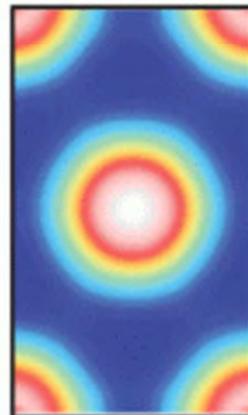
# Micro- and nanoscale PNCs



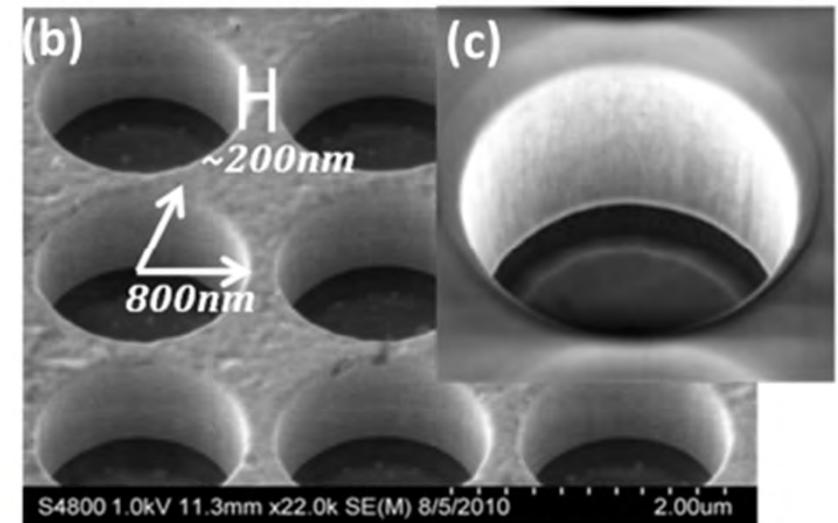
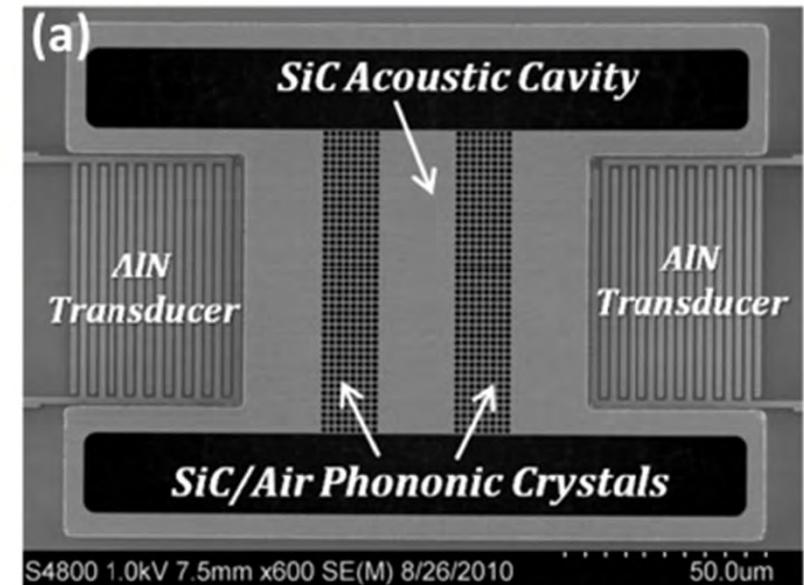
# Micro- and nanoscale PNCs



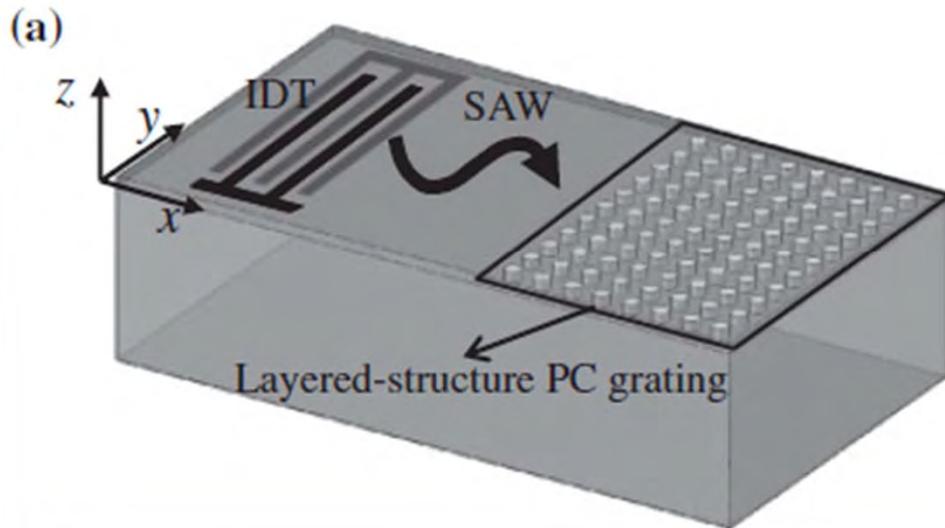
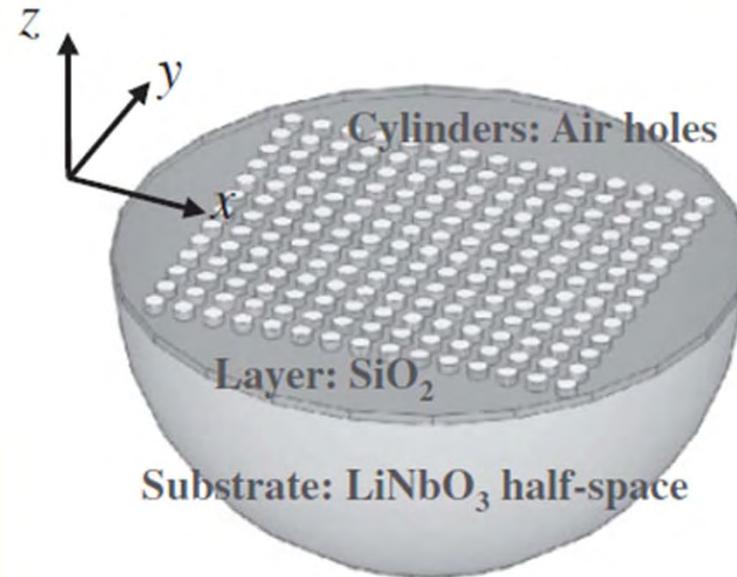
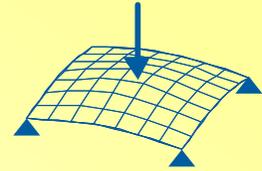
gold nanovoids



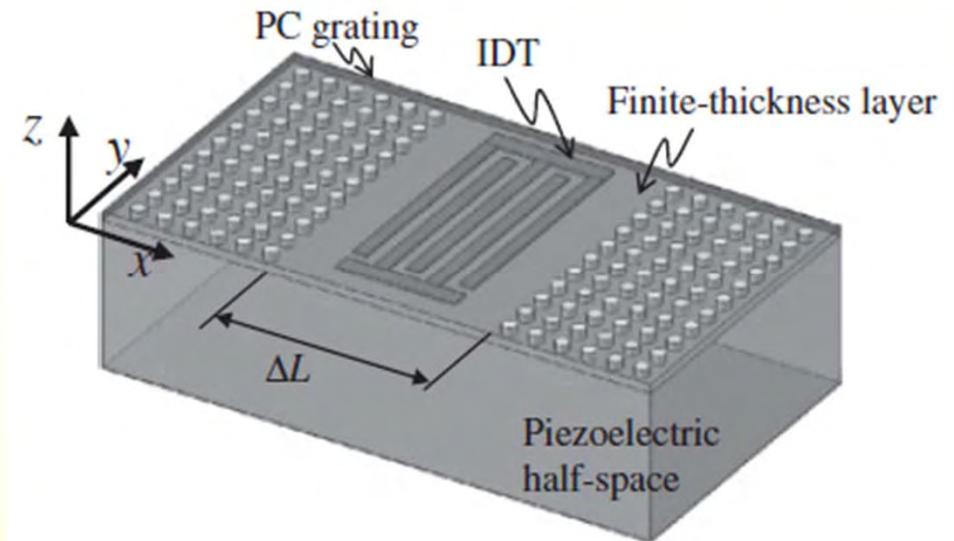
0.73  
GHz



# Surface acoustic waves in PNCs

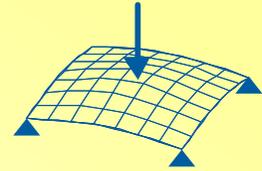


**SAW reflector**



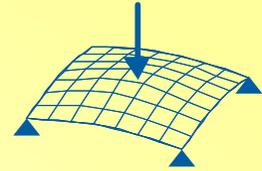
**SAW resonator**

Visiting Professors' College STU, Bratislava, Slovakia, 14 May 2015



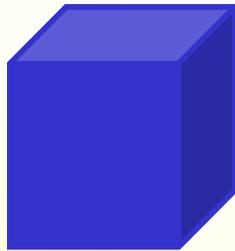
# Smart materials and structures

# Smart materials and structures



Mechanical energy

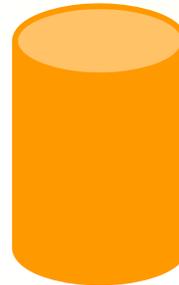
Piezoelectricity



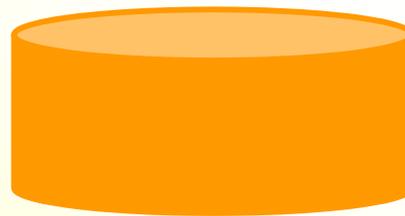
Electrical field



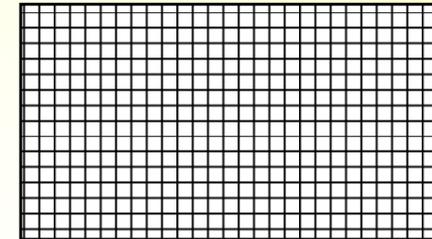
Magnetostrictive materials



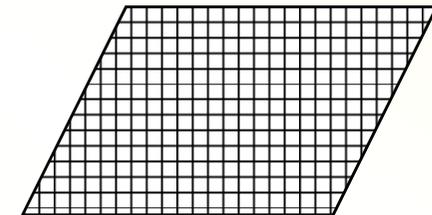
Magnetization



Shape memory alloy



Temperature



Actuator

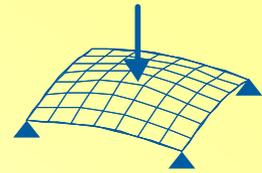
Sensor

Electrical energy

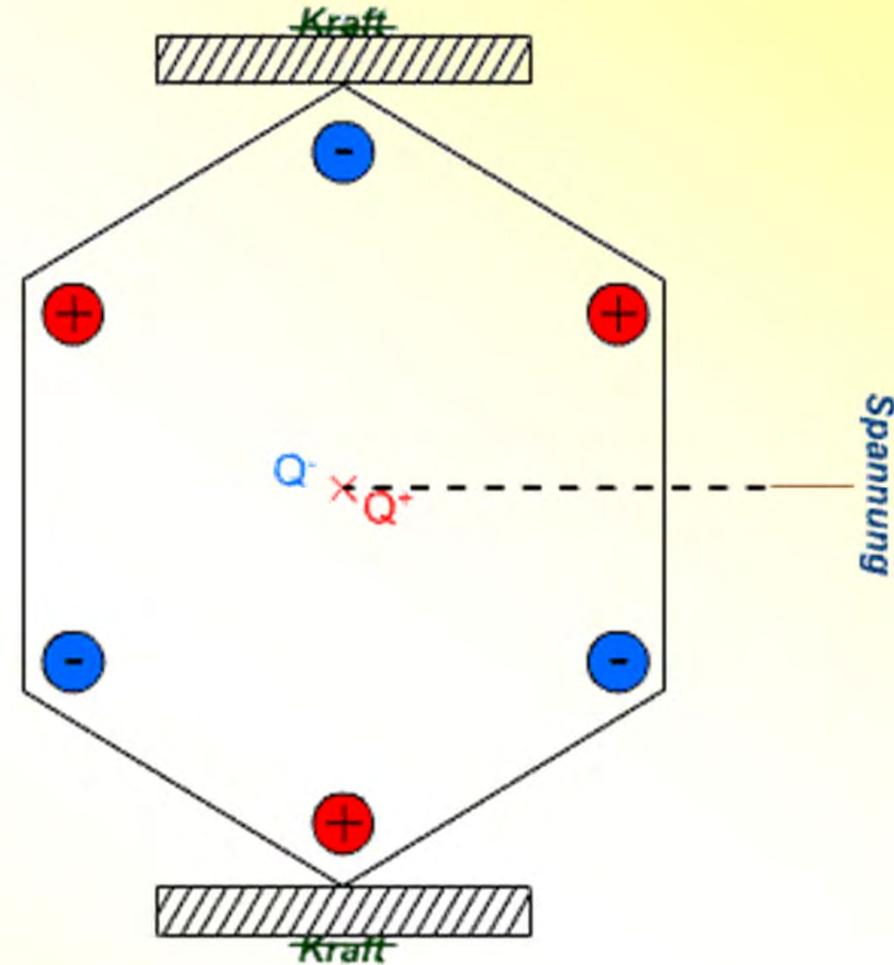
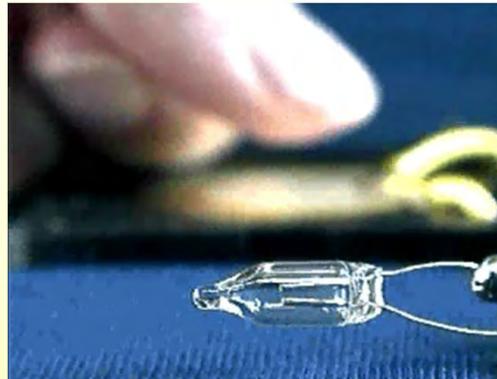
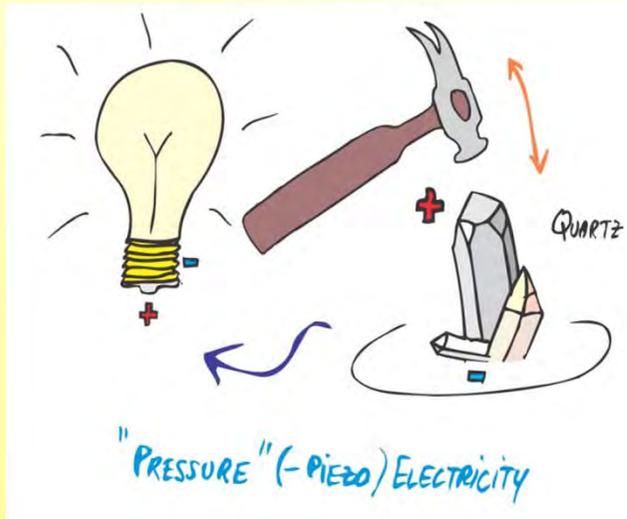
Magnetic energy

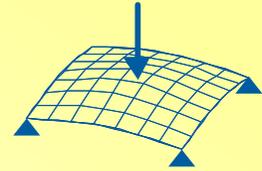
Thermal energy

# Smart materials and structures



Pierre and Jacques Curie: 1880

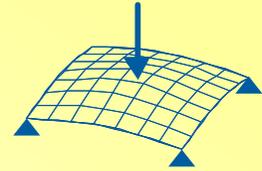




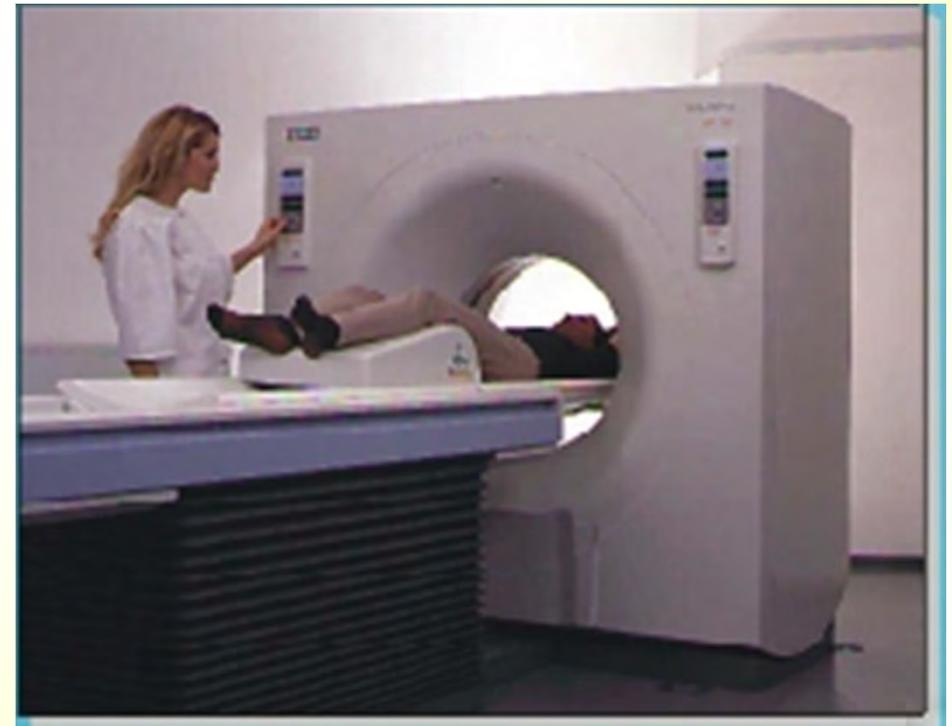
## Applications:

- **Sensor**
- **Actuator**
- **Transducer**
- **Sonar technology**
- **Smart structures**
- **Structural Health Monitoring (SHM)**
- **Medical diagnostics**
- **Energy harvesting**
- **...**

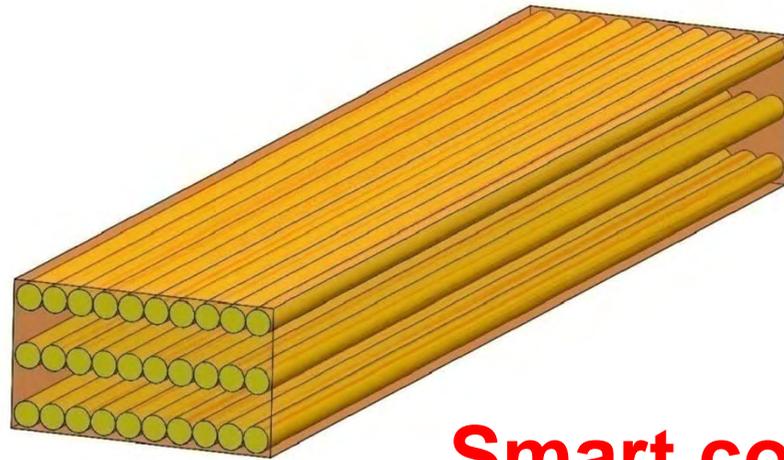
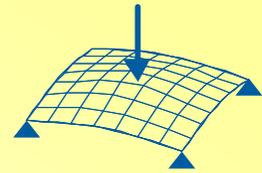
# Smart materials and structures



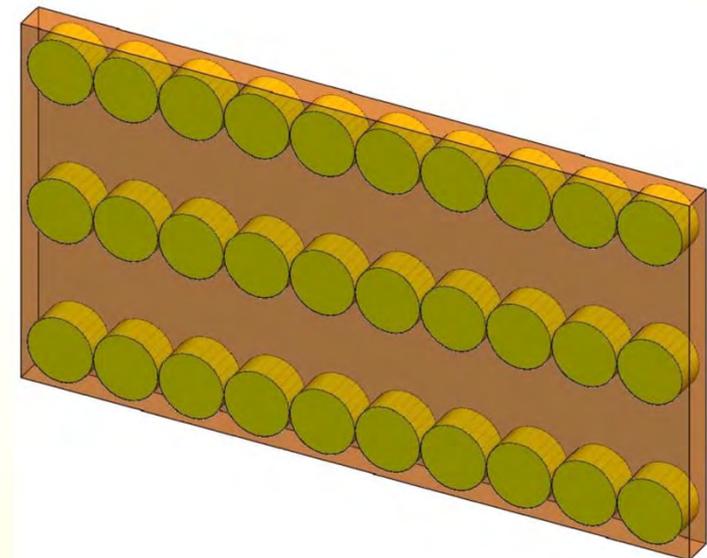
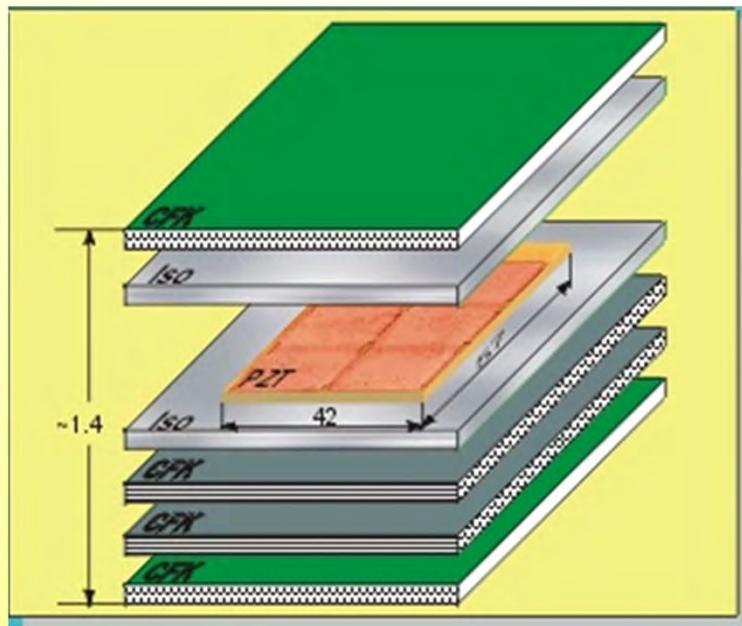
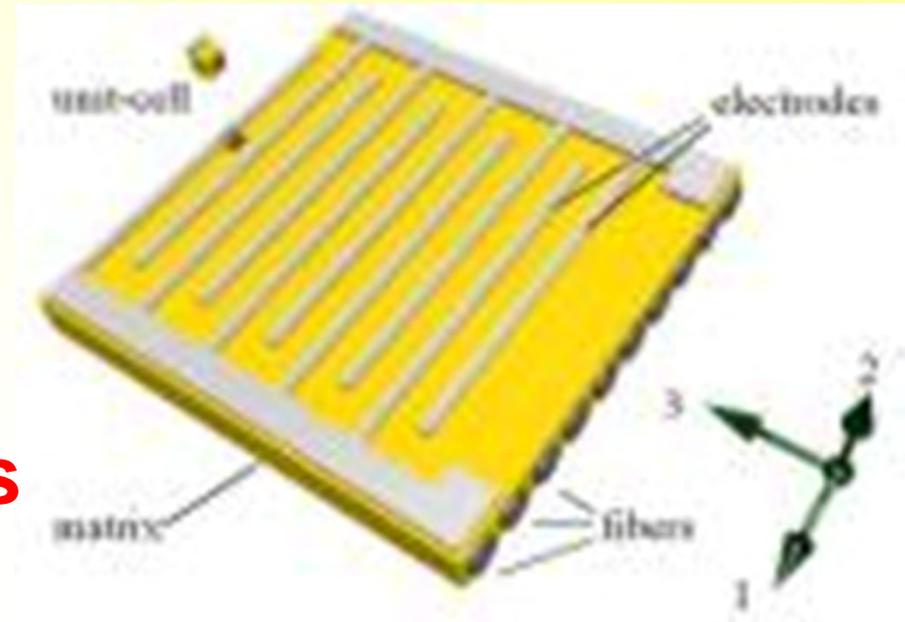
Piezokeramischer  
Luftultraschallwandler  
(Sender/Empfänger)



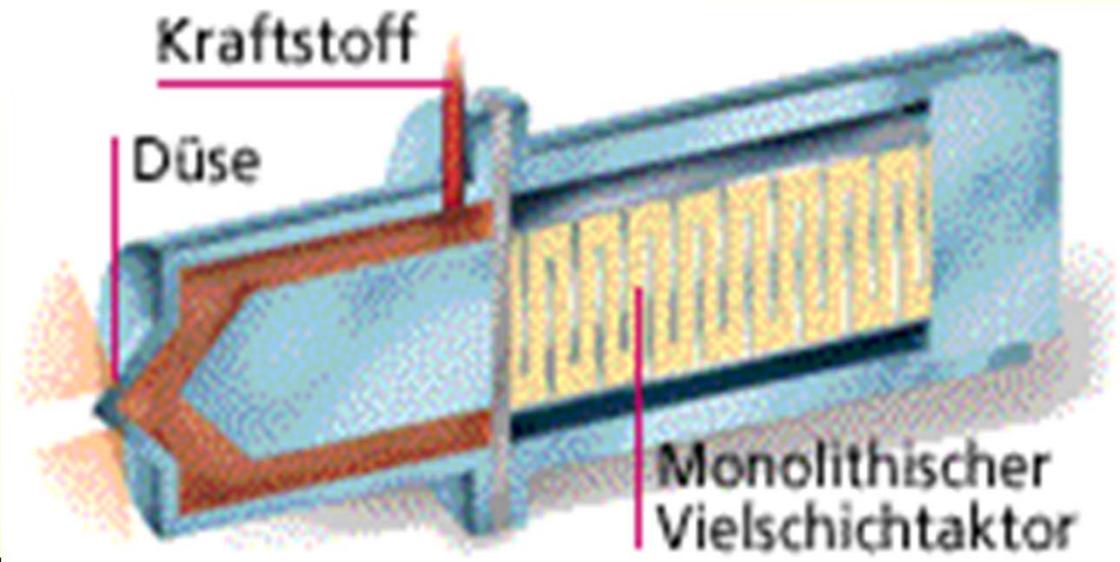
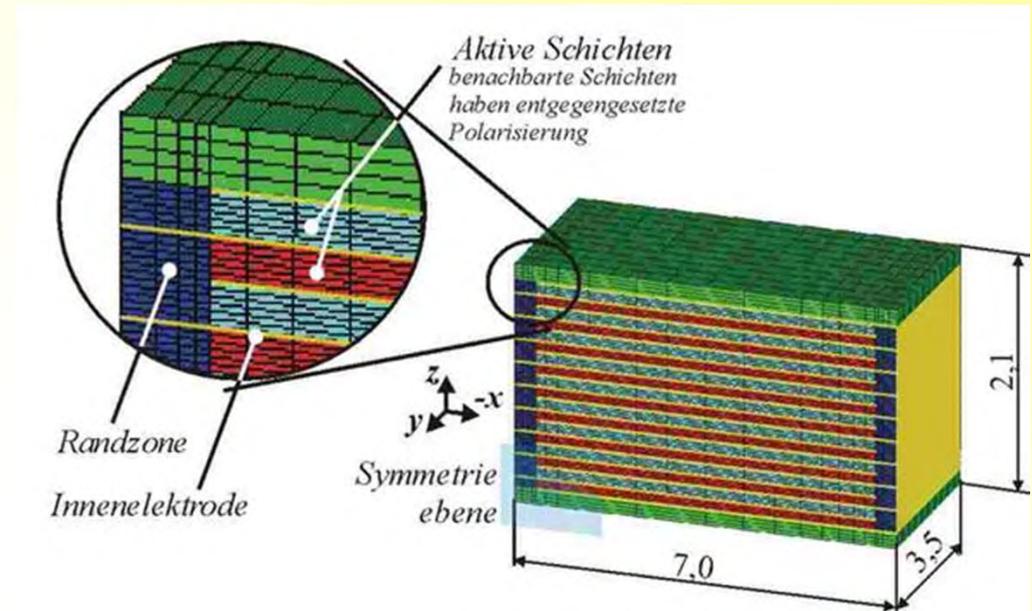
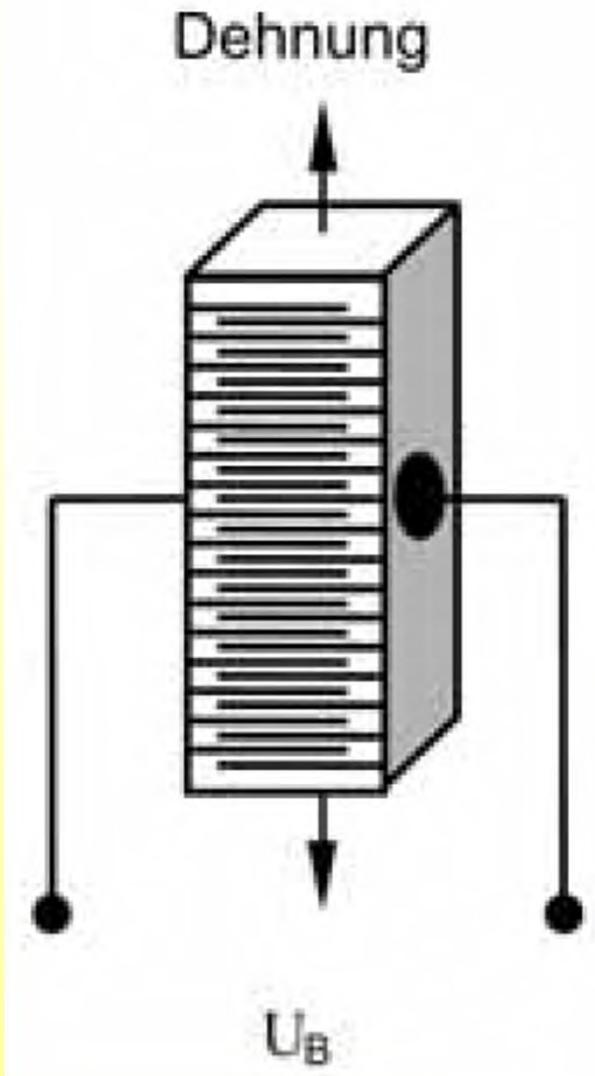
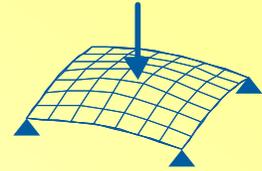
# Smart materials and structures



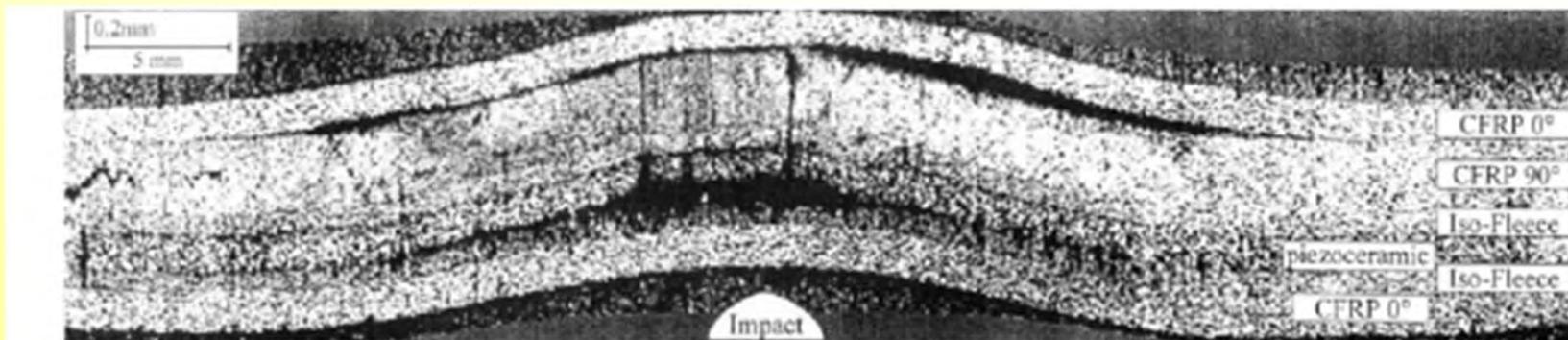
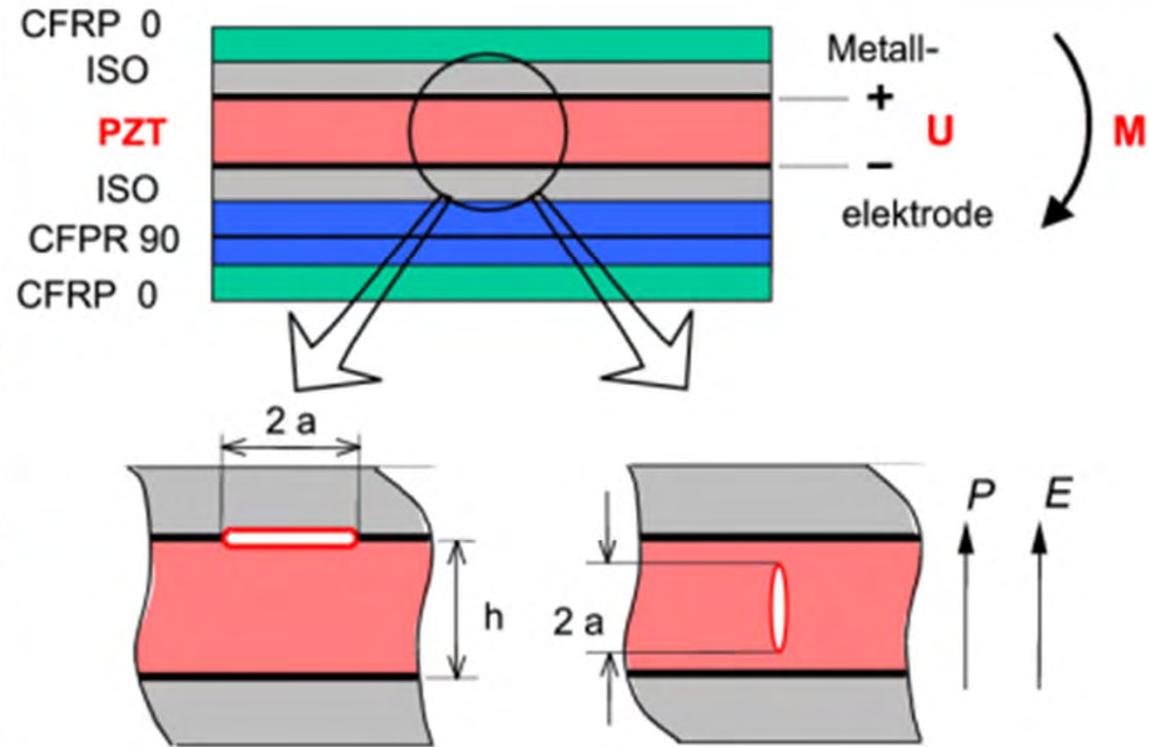
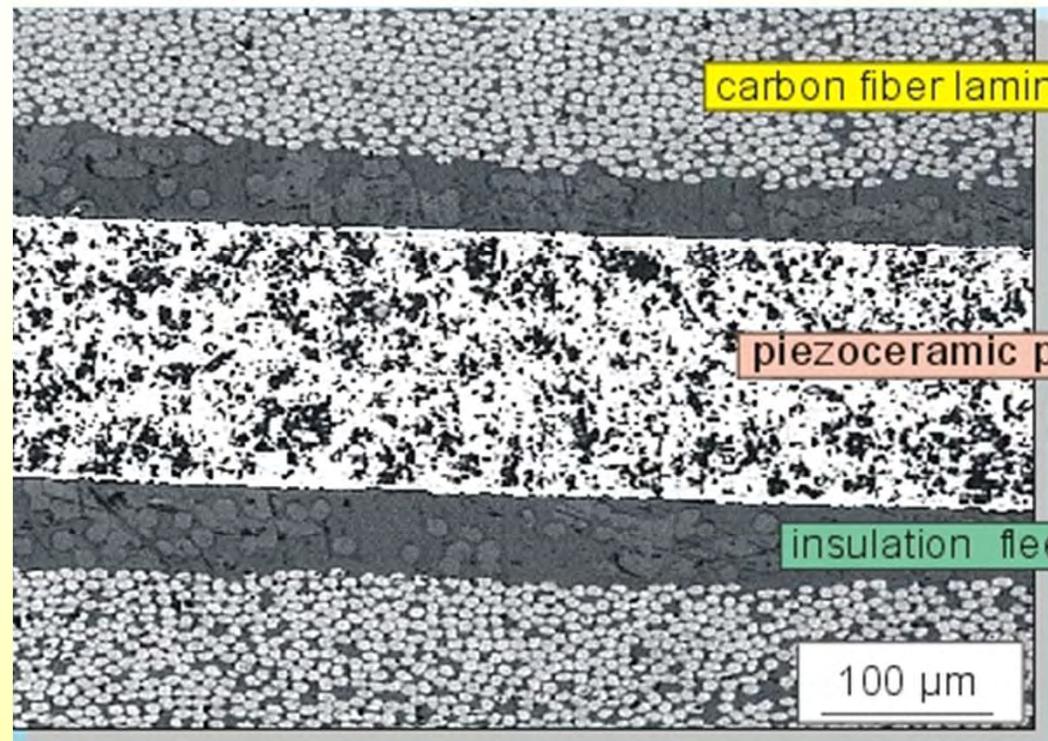
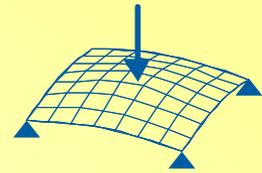
**Smart composites**

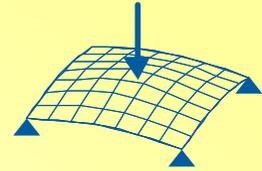


# Smart materials and structures



# Smart materials and structures



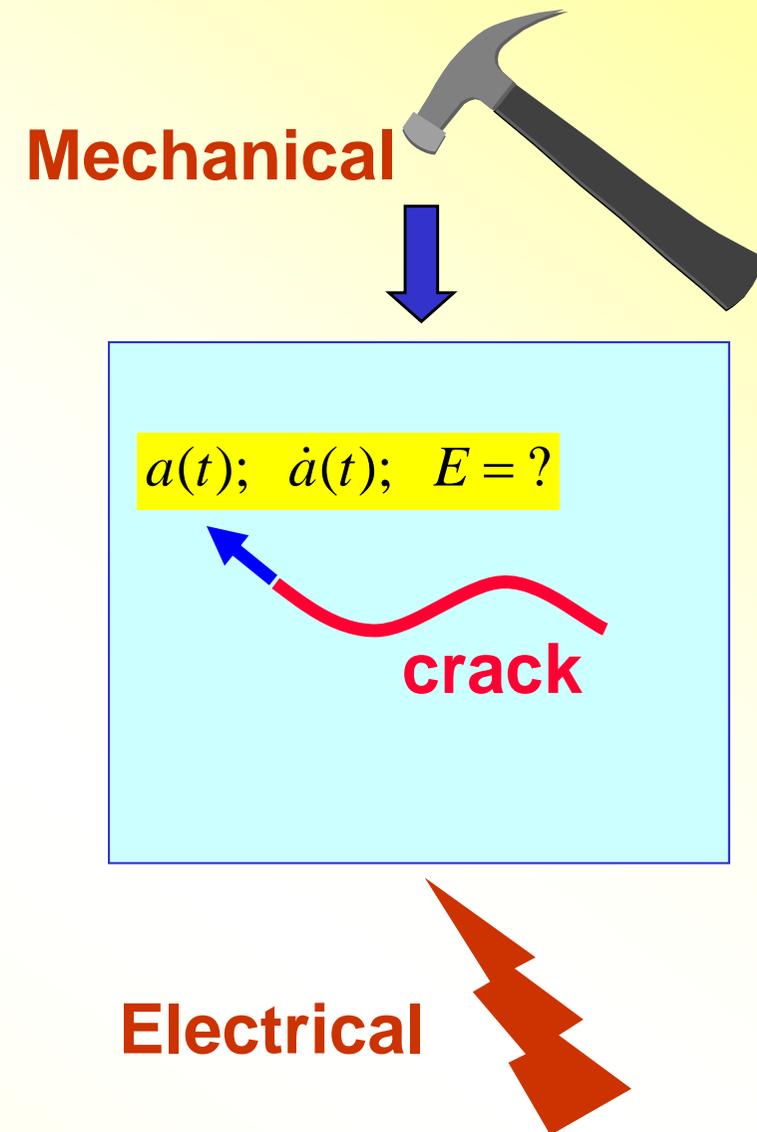


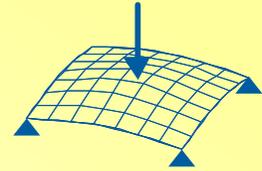
## Effects on crack propagation ?

- Crack initiation ?
- Crack growth velocity & direction ?
- Crack arrest through electrical loading ?

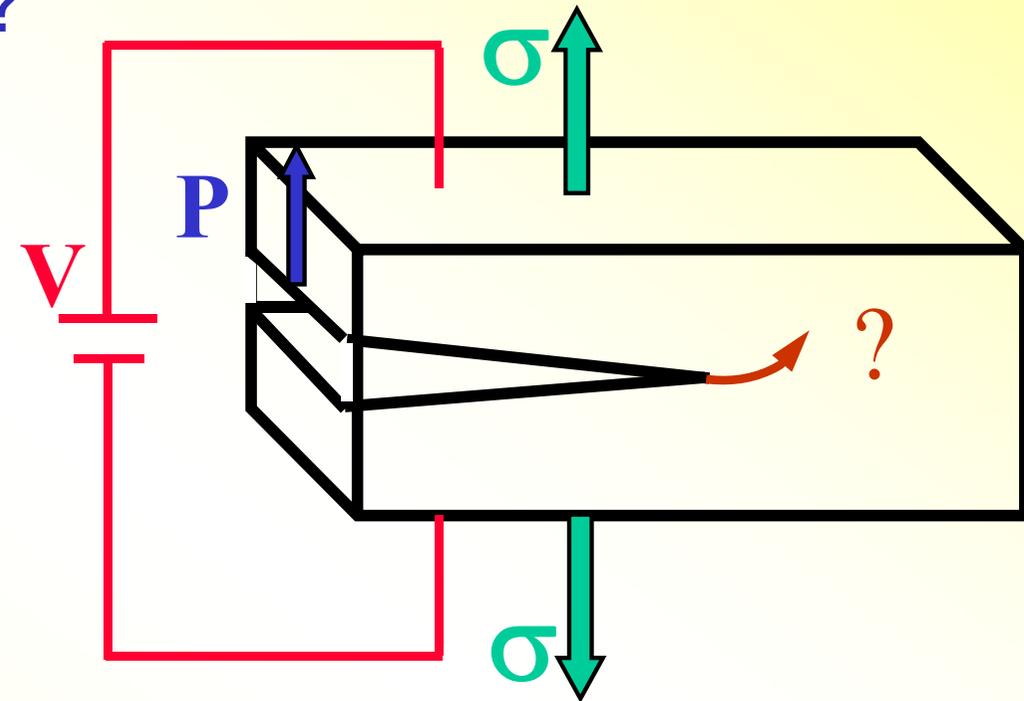
## Disturbance of electric signals ?

- Loss of functionality and reliability ?
- Adaptivity through mechanical loading ?

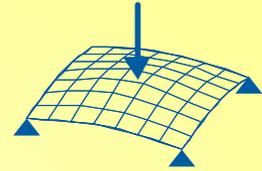




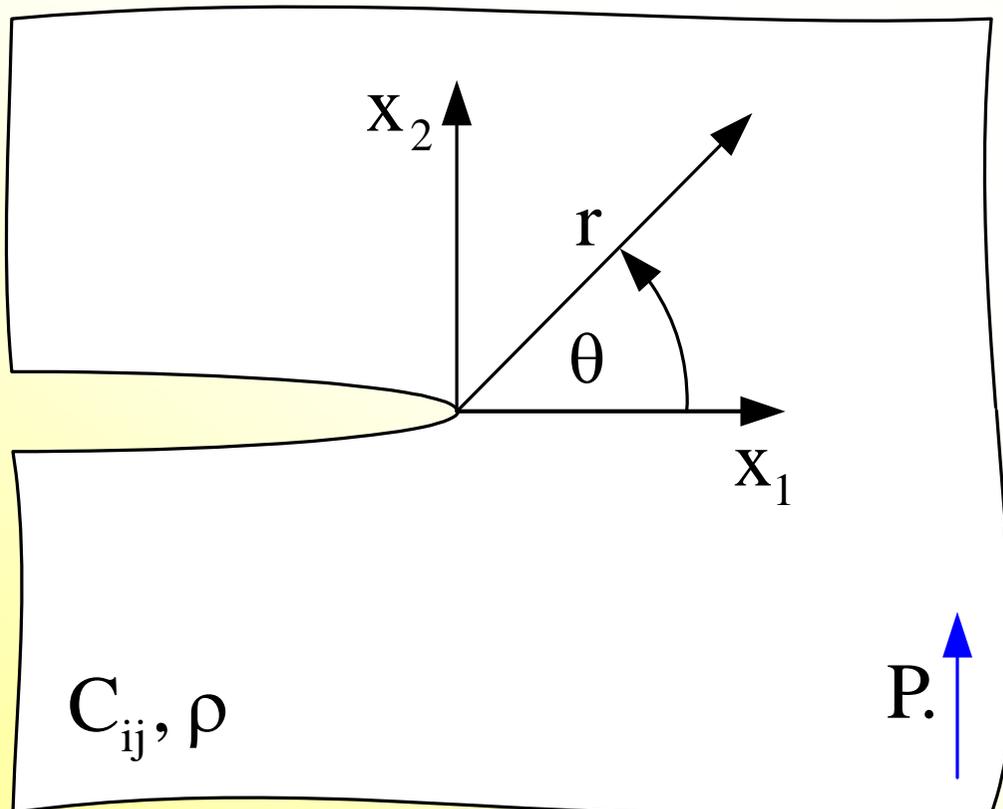
- Effect of the dynamic loading ?
- Effect of the interface ?
- Influence of the material mismatch ?
- Effect of the poling direction ?
- Influence of the loading combination ?



# Crack characterization



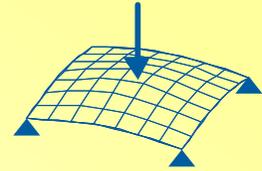
## Crack-tip field and intensity factors (interior crack)



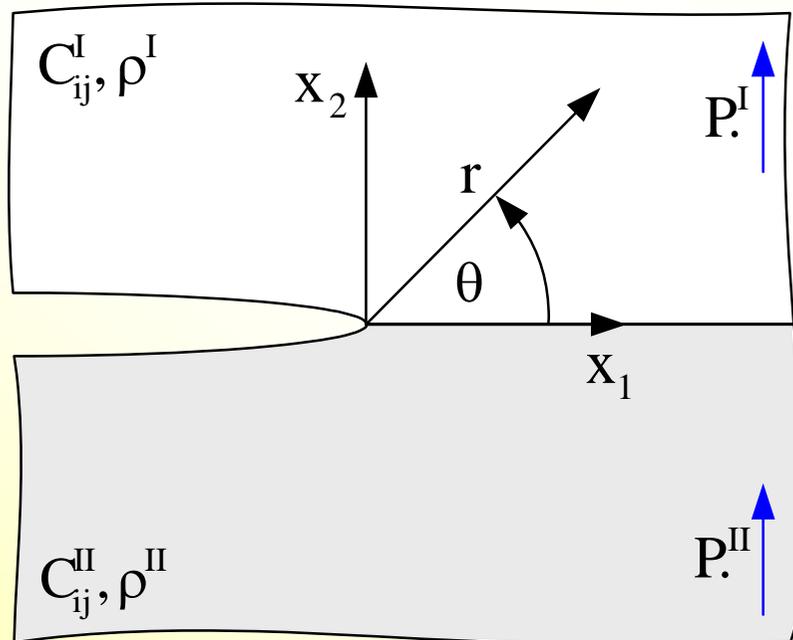
$$u_i \sim \sqrt{r}, \quad \varphi \sim \sqrt{r}$$
$$\sigma_{ij} \sim \frac{1}{\sqrt{r}}, \quad D_i \sim \frac{1}{\sqrt{r}}$$

$$\begin{Bmatrix} K_{II}(t) \\ K_I(t) \\ K_{IV}(t) \end{Bmatrix} = \sqrt{\frac{2\pi}{l}} \mathbf{H} \begin{Bmatrix} \Delta u_1(l, t) \\ \Delta u_2(l, t) \\ \Delta \varphi(l, t) \end{Bmatrix}$$

# Crack characterization



## Crack-tip field and intensity factors (interface crack)



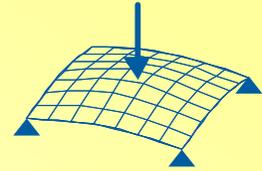
$$u_i \sim r^{\frac{1}{2}+i\varepsilon_1}, \quad \varphi \sim r^{\frac{1}{2}-\varepsilon_2}$$

$$\sigma_{ij} \sim r^{-\frac{1}{2}+i\varepsilon_1}, \quad D_i \sim r^{-\frac{1}{2}+\varepsilon_2}$$

$$\Delta \mathbf{u}(\mathbf{r}) = (\mathbf{H} + \bar{\mathbf{H}}) \sqrt{\frac{r}{2\pi}} \left[ \frac{\mathbf{K} r^{i\varepsilon_1} \mathbf{w}}{(1 + 2i\varepsilon_1) \cosh(\pi\varepsilon_1)} + \frac{\bar{\mathbf{K}} r^{-i\varepsilon_1} \bar{\mathbf{w}}}{(1 - 2i\varepsilon_1) \cosh(\pi\varepsilon_1)} + \frac{\mathbf{K}_4 r^{-\varepsilon_2} \mathbf{w}_4}{(1 - 2\varepsilon_2) \cos(\pi\varepsilon_2)} \right]$$

$$\boldsymbol{\sigma}(\mathbf{r}) = \frac{1}{\sqrt{2\pi r}} \left[ \mathbf{K} r^{i\varepsilon_1} \mathbf{w} + \bar{\mathbf{K}} r^{-i\varepsilon_1} \bar{\mathbf{w}} + \mathbf{K}_4 r^{-\varepsilon_2} \mathbf{w}_4 \right]$$

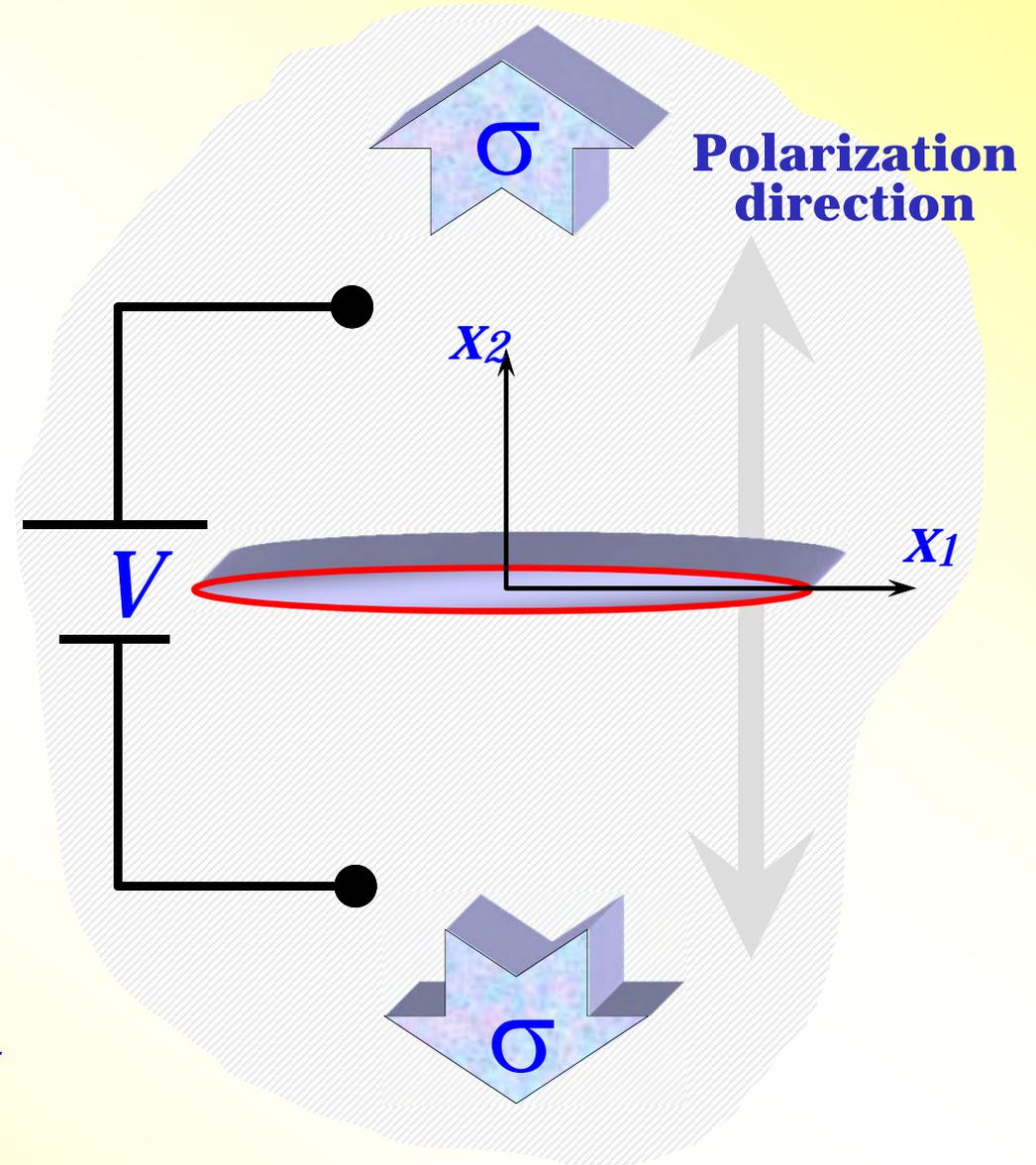
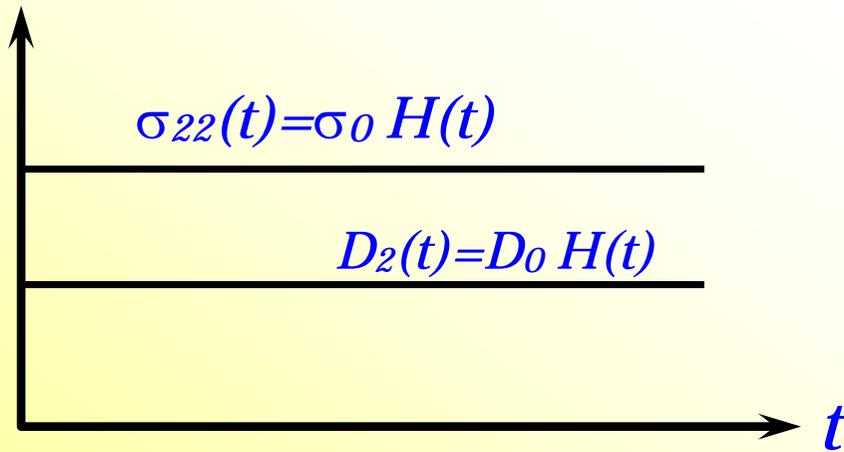
# Examples



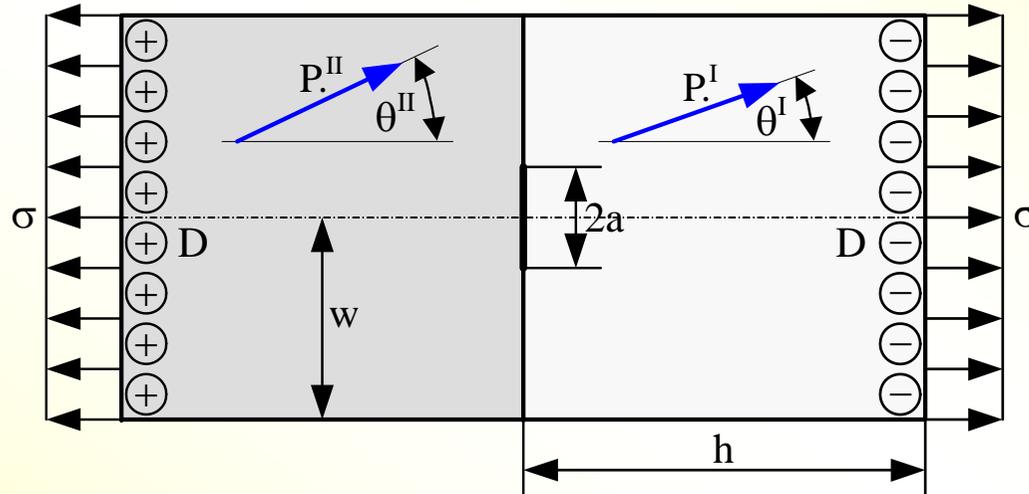
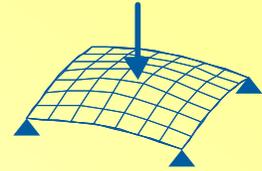
## Loading parameter

$$\chi = \frac{e_{22}}{\epsilon_{22}} \frac{D_2}{\sigma_{22}}$$

Load



# Examples



## Geometry:

$$h = 20\text{mm}, \quad 2w = h, \quad 2a = 4.8\text{mm}$$

## Loading:

$\sigma$ : mechanical

$D$ : electrical

## Material I: PTZ-5H

$$C_{11} = 126.0\text{GPa}, \quad C_{12} = 53.0\text{GPa}$$

$$C_{22} = 117.0\text{GPa}, \quad C_{66} = 35.3\text{GPa}$$

$$e_{21} = -6.5\text{C/m}^2, \quad e_{22} = 23.3\text{C/m}^2,$$

$$e_{16} = 17.0\text{C/m}^2$$

$$\varepsilon_{11} = 15.04\text{C}/(\text{GVm}), \quad \varepsilon_{22} = 13.0\text{C}/(\text{GVm})$$

## Material II: BaTiO<sub>3</sub>

$$C_{11} = 150.0\text{GPa}, \quad C_{12} = 66.0\text{GPa}$$

$$C_{22} = 146.0\text{GPa}, \quad C_{66} = 44.0\text{GPa}$$

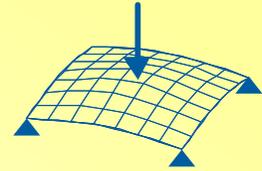
$$e_{21} = -4.35\text{C/m}^2, \quad e_{22} = 17.5\text{C/m}^2$$

$$e_{16} = 11.4\text{C/m}^2$$

$$\varepsilon_{11} = 9.87\text{C}/(\text{GVm}), \quad \varepsilon_{22} = 11.2\text{C}/(\text{GVm})$$

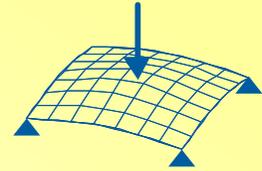
**A rectangular plate with a central interface crack**

# Key questions



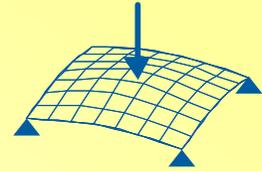
- Effect of the interface ?
- Effect of the polling direction ?
- Effect of the material mismatch ?
- Effect of the electrical loading ?
- Effect of the mechanical loading ?
- Effect of the dynamic loading (impact) ?
- Effect of the loading combination ?

Visiting Professors' College STU, Bratislava, Slovakia, 14 May 2015



# Conclusions

# Conclusions



- New discoveries of multifunctional materials and structures will lead to promising and exciting fundamental breakthroughs. 😄
- Transfer of scientific knowledge and principles to engineering technologies is important and demanding. 🤔
- Cutting edge applications of novel multifunctional materials and structures are important for the sustainable development. 😄
- Novel multifunctional materials and structures will greatly influence our society, economy and ecology (environment). 😄
- Novel multifunctional materials and structures will improve our life quality and make our life happy! 😄👍